



## DICTRA On-line Training

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[www.thermocalc.com](http://www.thermocalc.com)

## Diffusion Module (DICTRA)

### Day 1

9:00	Introduction to DICTRA (= Diffusion Module)
9:40	<b>Example</b> - Up-hill diffusion in the Fe-Si-C system
10:25	Q&A
10:40	<b>Example</b> – Carburisation and de-carburisation
11:10	<b>Example</b> – Particle growth
11:45	Q&A
12:00	Home assignment 1

Download material for today:

<https://download.thermocalc.com/courses/Diff-Day1/>

## Diffusion Module (DICTRA)

### Day 2

- 9:00 Home assignment 1
- 9:10 **Example** - Solidification using Scheil
- 9:30 **Example** - Scheil with real back-diffusion in the solid.
- 9:50 **Example** – DICTRA solidification (Moving phase boundary)
- 10:30 Q&A
- 10:45 Diffusion theory and numerics
- 11:15 **Example** – Homogenisation model: Diffusion couple
- 11:45 Q&A
- 12:00 Home assignment 2

## Diffusion Module (DICTRA)

### Day 3

9:00	Home assignment 2
9:10	<b>Example</b> – Dissolution of cementite particles (moving phase boundary calculation)
10:10	Console mode and macro files.
10:30	Q&A
10:45	<b>Example</b> – Gradient sintering in Cemented carbide
11:30	Trouble shooting
11:45	Q&A
12:00	End

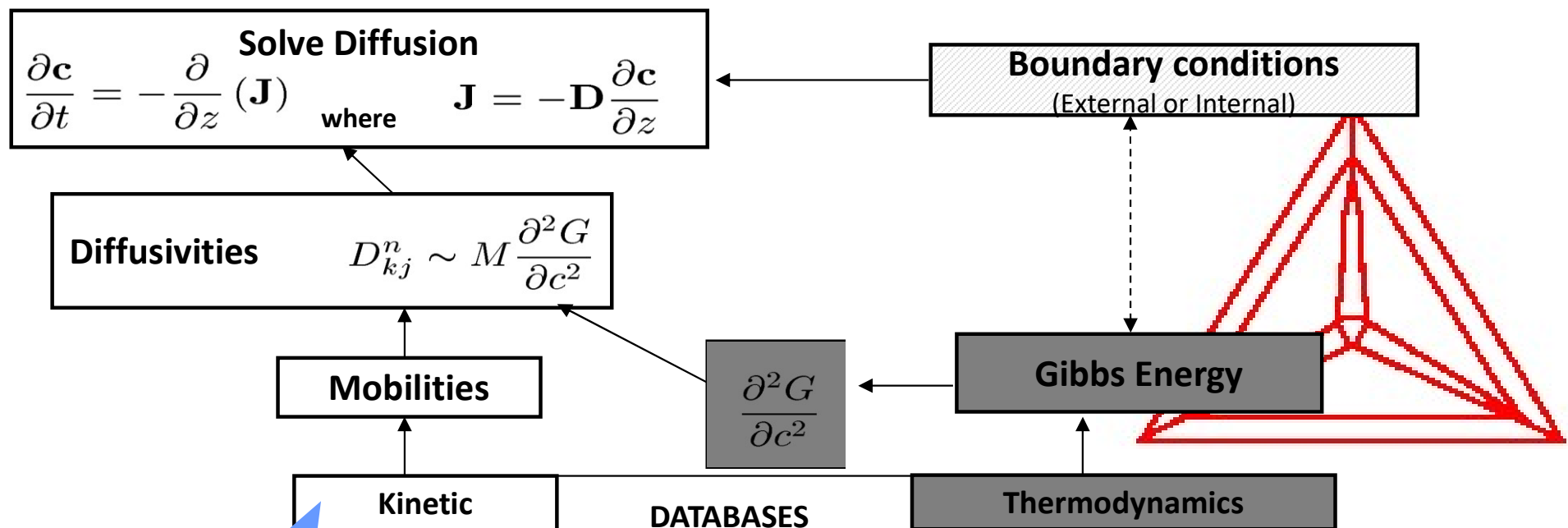
# The Software



- ❑ Software package for simulation of diffusion controlled reactions in multi-component alloys.
- ❑ Simulation on geometries, which may be reduced to one spatial coordinate (planar, cylindrical or spherical)
- ❑ Linked to Thermo-Calc, which provides all necessary thermodynamic properties.
- ❑ Development started over 35 years ago at:
  - Royal Institute of Technology in Stockholm, Sweden
  - MPI für Eisenforschung in Düsseldorf, Germany (only very early)
  - Thermo-Calc Software AB (from 1997 and on)

# Basic calculation procedure

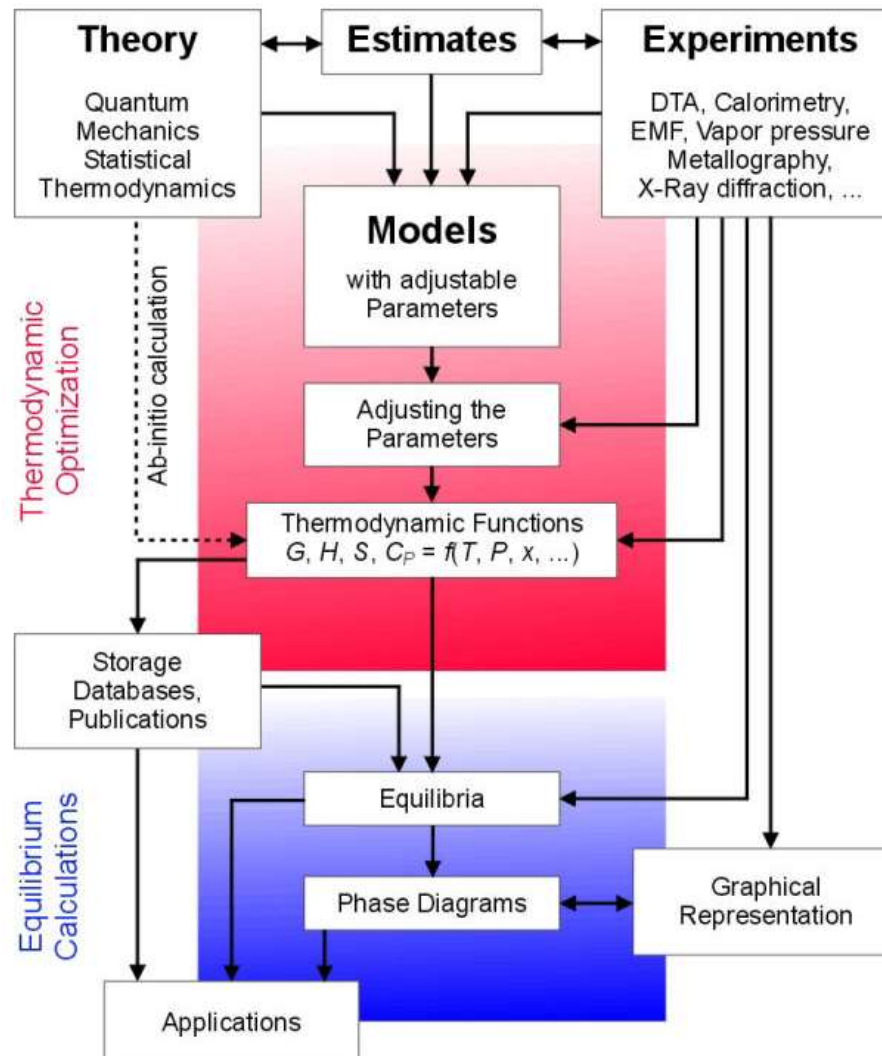
*A numerical finite difference scheme is used for solving a system of coupled parabolic partial differential equations*



Why a database with Mobilities?

*All simulations depend on assessed kinetic and thermodynamic data, which are stored in databases*

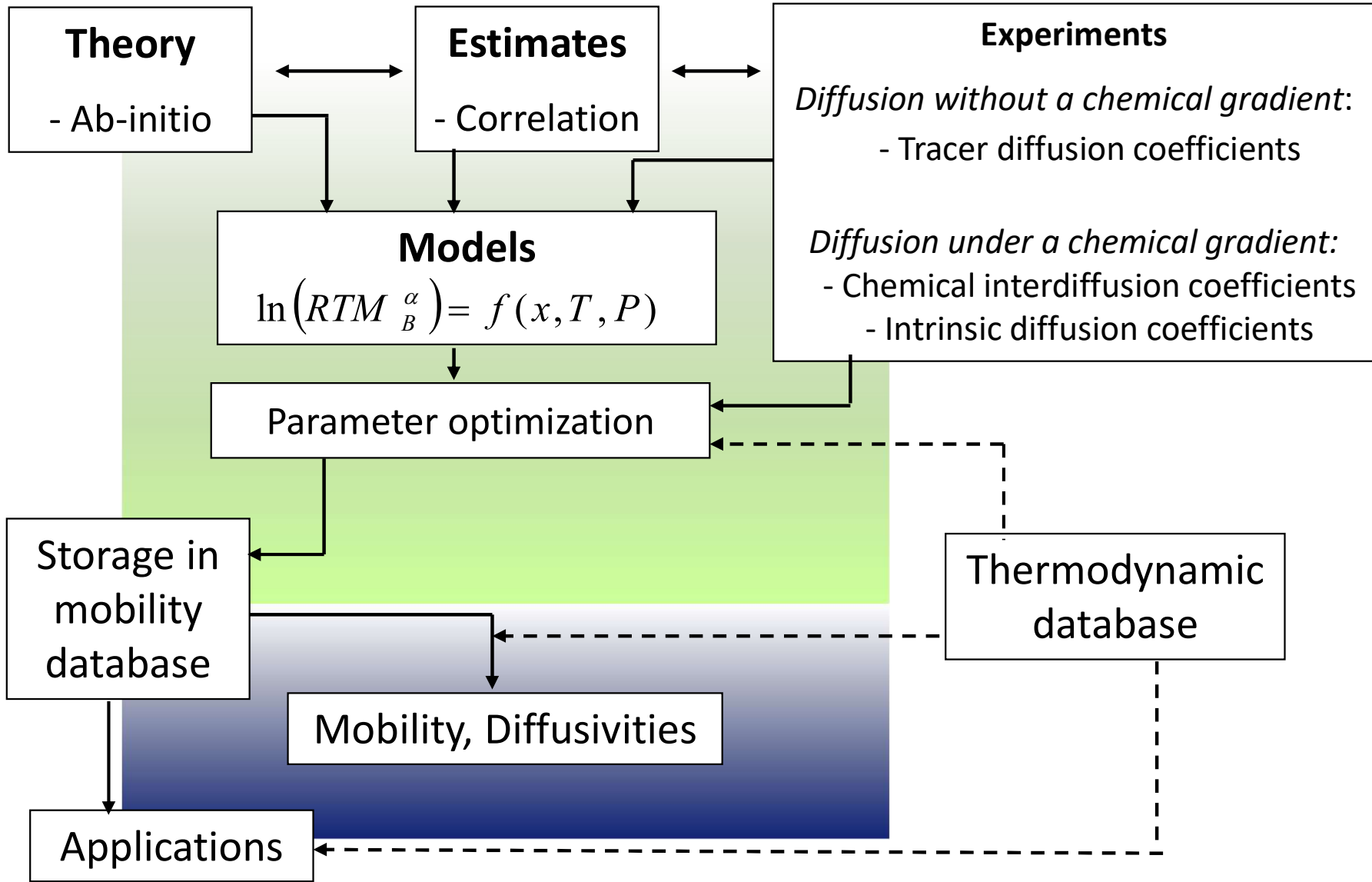
# Thermodynamic Databases (*The CALPHAD approach*)



# Kinetic Databases (*in a CALPHAD spirit*)

Assessment and optimization

Prediction





# Modelling of the atomic mobility

From absolute reaction-rate theory arguments Andersson and Ågren<sup>1)</sup> suggested:

$$M_B = M_B^0 \exp\left(\frac{-Q_B}{RT}\right) \frac{1}{RT} \quad \left\{ \begin{array}{l} M_B \text{ Mobility for element } B \\ M_B^0 \text{ Frequency factor} \\ Q_B \text{ Activation energy} \end{array} \right.$$

When treating the composition dependency of the mobility, Jönsson<sup>2)</sup> found it superior to expand the logarithm of the mobility rather than the value itself, i.e.

$$RT \ln [RT M_B] = RT \ln M_B^0 - Q_B$$

Because  $\ln [RT M_B]$  is often found to have a fairly linear composition dependency

1. Andersson, Ågren, *J Appl Phys* 72(1992)1350

2. Jönsson, *Scand J Metall* 24(1995)21

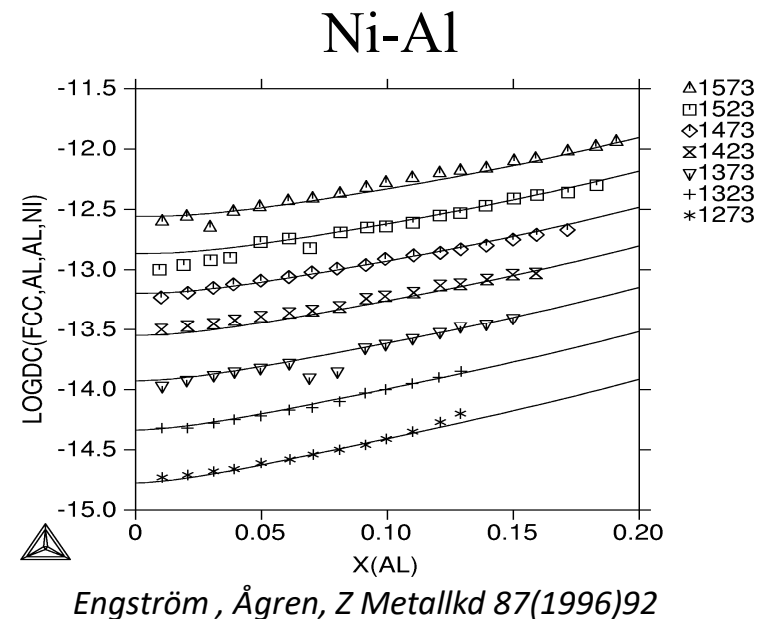
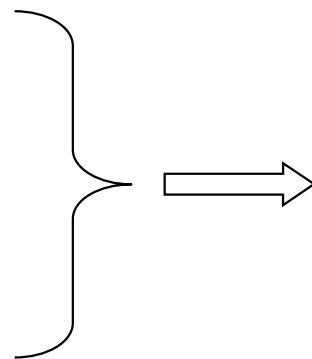
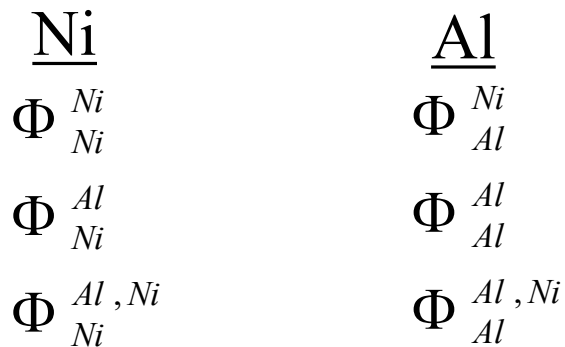
# Composition dependency

In a CALPHAD spirit the composition dependency is represented with a linear combination of the values at each endpoint of the composition space, and a Redlich-Kister expansion, i.e.

$$\Phi_B = \sum_i x_i \Phi_B^i + \sum_i \sum_{j>i} x_i x_j \left[ \sum_{r=0}^m {}^r \Phi_B^{i,j} (x_i - x_j)^r \right]$$

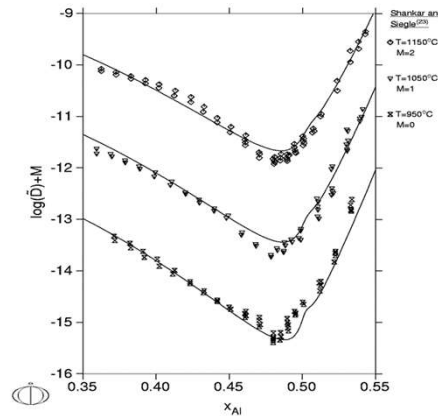
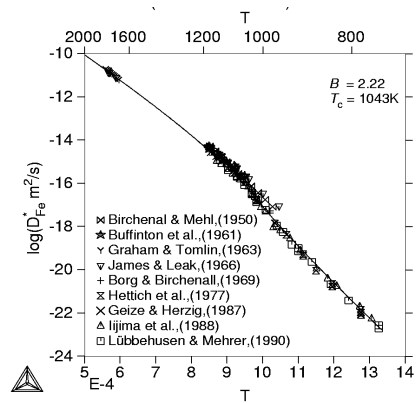
where  $\Phi_B$  represents  $RT \ln M_B^0 - Q_B$

Example: FCC Ni-Al




# Other effects on mobility

- ✓ Ferromagnetic ordering
  - ✓ Chemical ordering
- can have very strong effects on the mobility and are described by a separate term each in the mobility expression.




Mobility enhancement in grain boundaries or dislocations are not taken into account in the mobility databases. It can be handled in the software by entering cross sectional area fractions and a factor reducing the activation energy compared to the bulk (console mode only).

# DICTRA application types

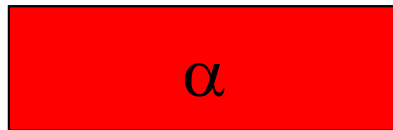
- Diffusion in single-phase systems
- Diffusion with moving interfaces
- Cell calculations (particle distributions, immobile interfaces etc.) – only in Console mode or use TC-PRISMA
- Diffusion in dispersed systems – only in Console mode, use
- Homogenization model 
- Coarsening or Ostwald ripening – use TC-PRISMA
- Growth of pearlite – Console mode, very little used.

# DICTRA application types

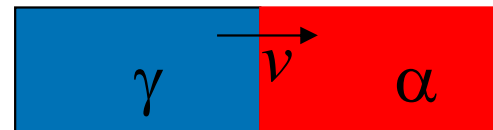
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- 

# DICTRA application types

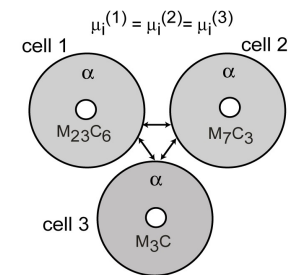
Single phase



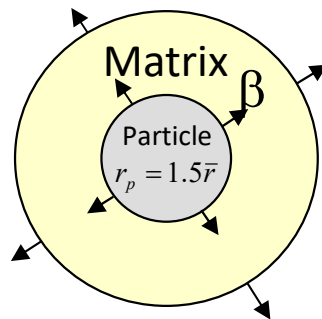
Moving boundary



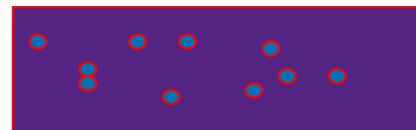
Cell



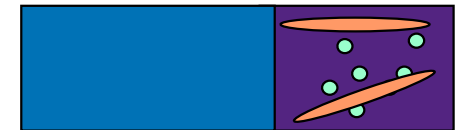
Coarsening



Disperse system

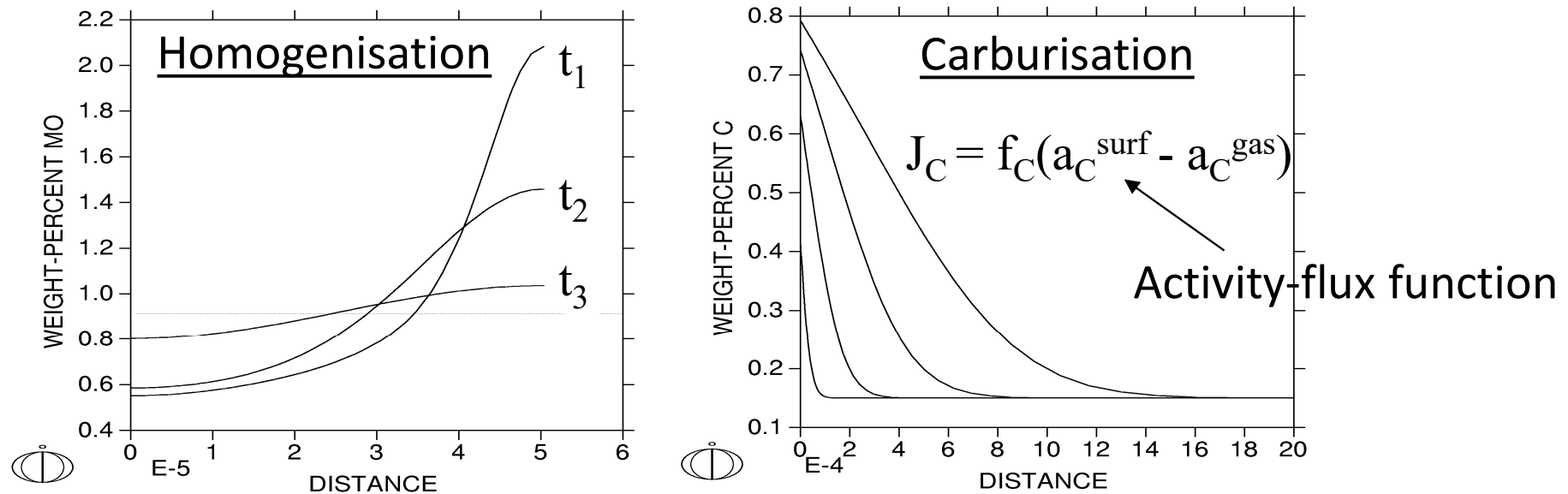


Homogenization



# Diffusion in single-phase systems

Straight-forward non-complex simulations, usually on homogenisation or carburisation treatments

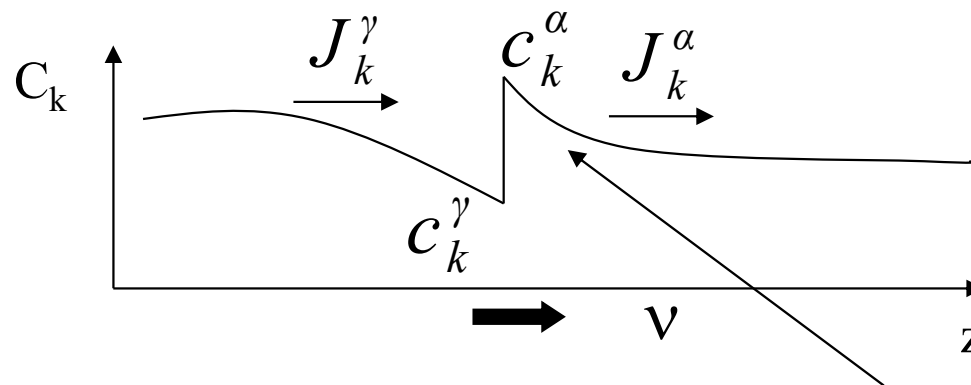


Boundary conditions can be specified as functions of time, temperature and pressure.

Different functions may be used in different time intervals.

*Also: Spatially non-isothermal simulations*

# Diffusion with a moving interface



n-1 unknowns:

n-2 chemical potentials.

Velocity of phase boundary,  $v$

*Sharp interface with  
assumption of local equilibrium  
(also para-equilibrium possible)*

n-1 Flux Balance Equations:

$$v (c_k^\alpha - c_k^\gamma) = J_k^\alpha - J_k^\gamma$$

F-B Equations solved as:

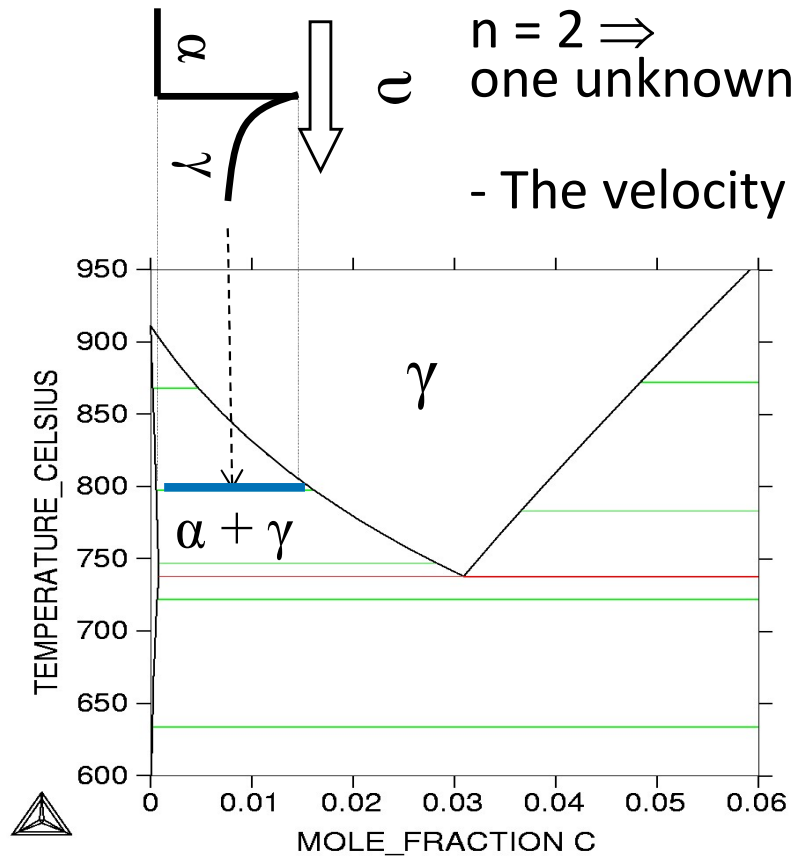
$$\sum_{k=1}^{n-1} [v (c_k^\alpha - c_k^\gamma) - (J_k^\alpha - J_k^\gamma)]^2 < \varepsilon$$



# Diffusion with a moving interface

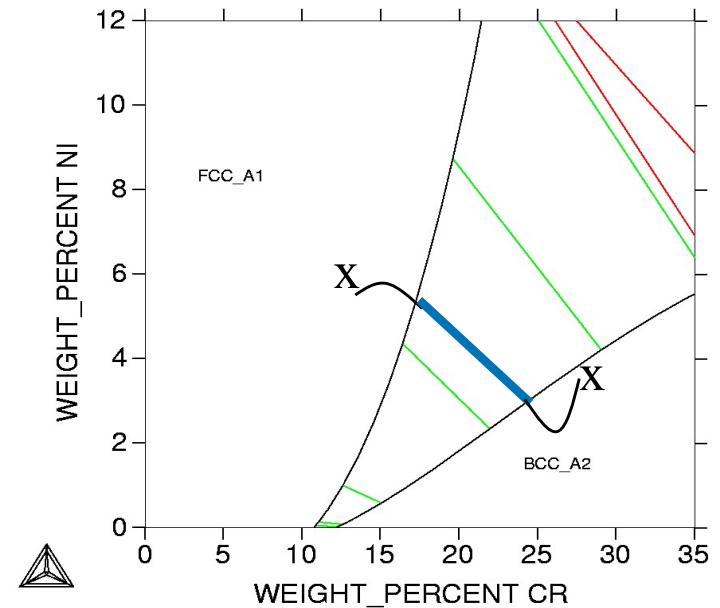
## Binary example: Fe-C

## Ternary example: Fe-Cr-Ni



$n = 3 \Rightarrow$  two unknowns!

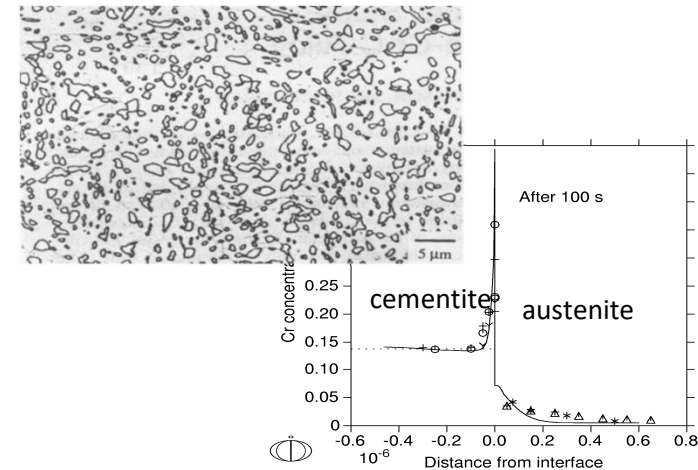
- One  $a_i$  or  $\mu_i$  (i.e. one tie-line)
- The velocity



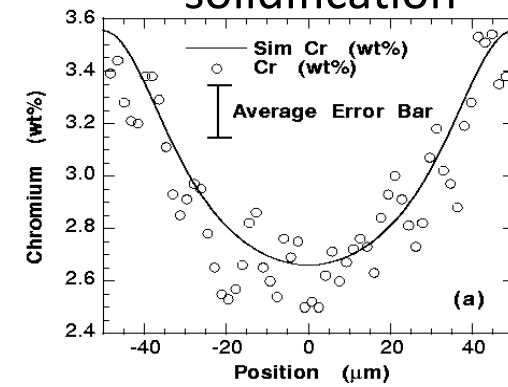
# Some application examples

- $\gamma$  to  $\alpha$  transformations in steel
- Growth and dissolution of particles
- Microsegregation during solidification
- $\sigma$ -phase precipitation in stainless steels
- Transient Liquid-Phase bonding of alloys
- Sintering of cemented carbides
- *and much more ...*

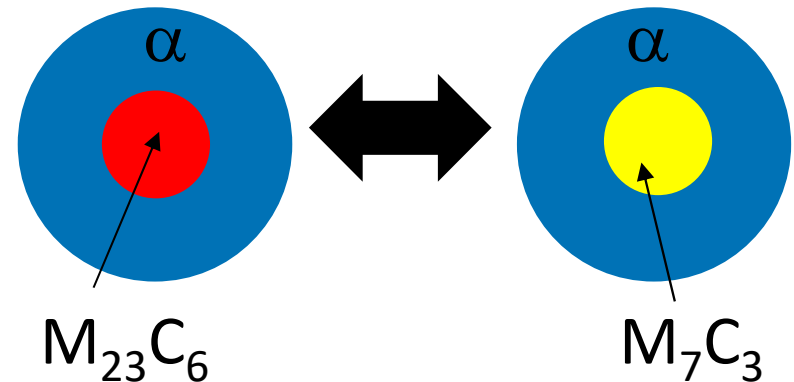
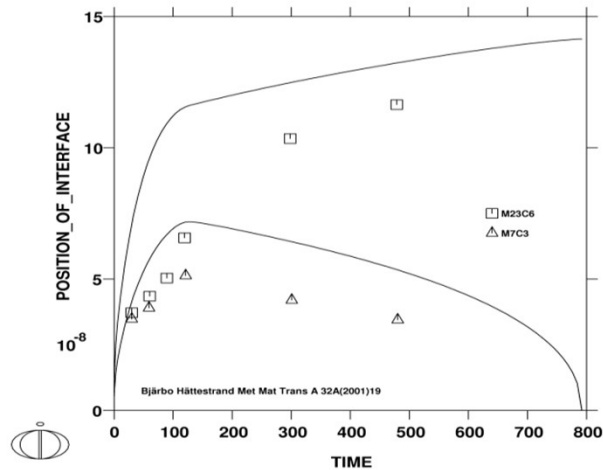
## Carbide dissolution



## Microsegregation during solidification



# Cell calculations



## Conditions for cell boundaries:

- Growth or dissolution of particle distributions
- Competing growth or dissolution
- Interdiffusion across an immobile interface

- ✓ Equal diffusion potentials  $\Phi_i$  for the elements

$$\Phi_i = \mu_i - \mu_n \quad \text{for subst. elements}$$

$$\Phi_i = \mu_i \quad \text{for interstitial elements}$$

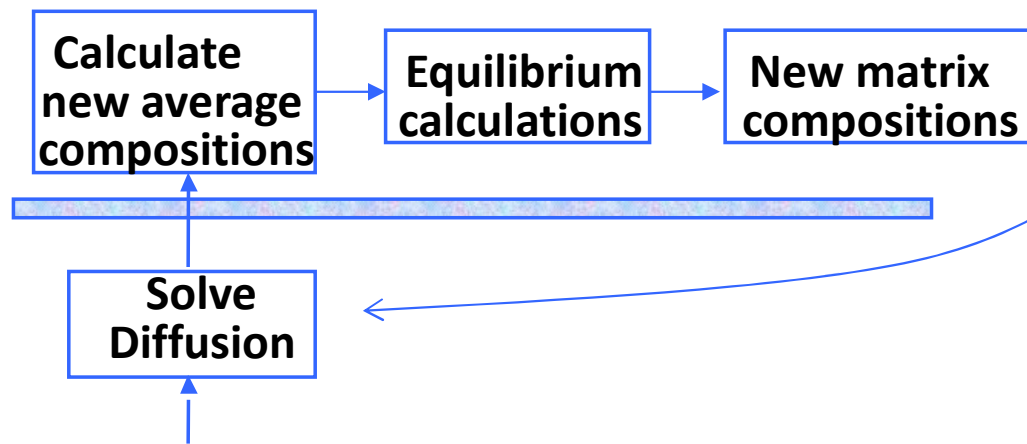
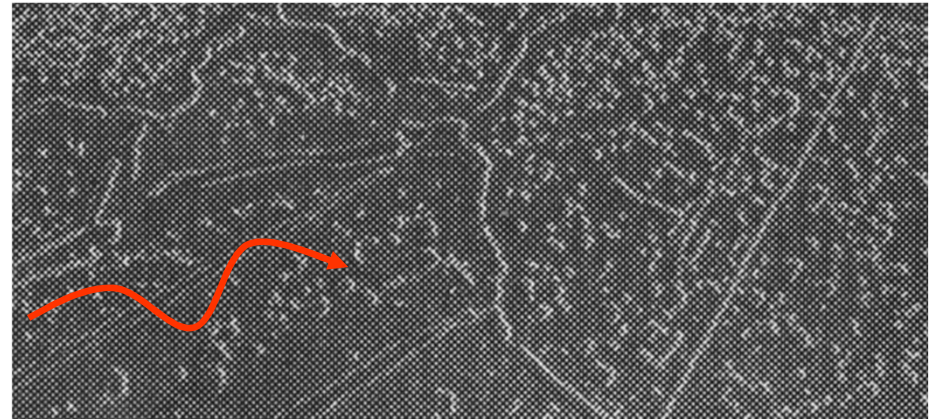
- ✓ Flux balances to conserve the mass of the elements

$$\frac{J_i^{\text{cell}\#1}}{n^{\text{cell}\#1}} = \frac{J_i^{\text{cell}\#2}}{n^{\text{cell}\#2}} \quad n, \text{ cell distribution factors}$$

# Diffusion in dispersed systems

## Assumptions:

- Diffusion takes place in the matrix phase only.
- Equilibrium holds locally in each node.



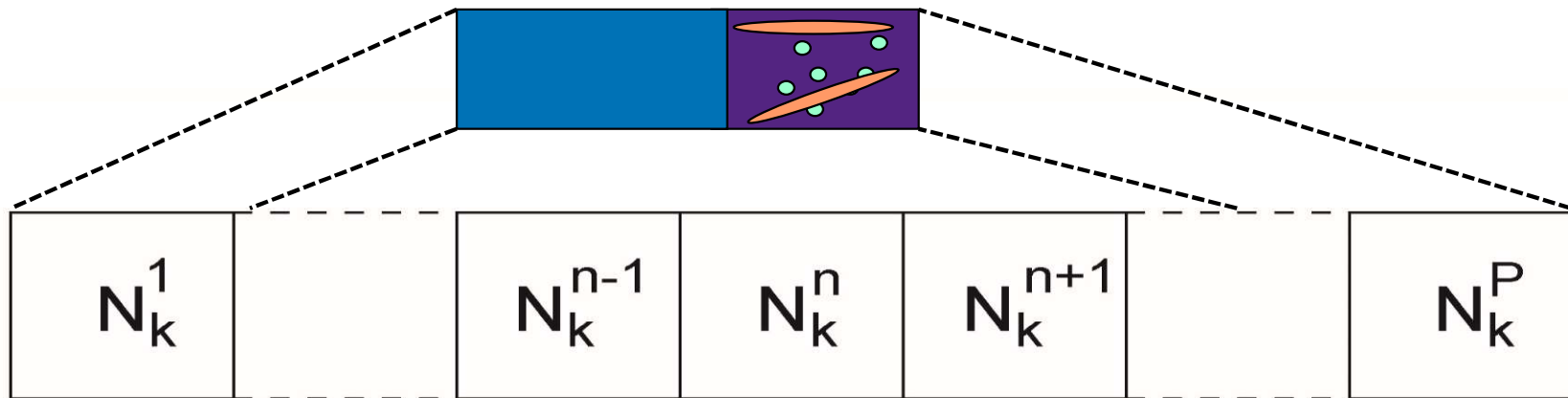
*A more general alternative:  
the homogenization model*

- Carburisation of high-temperature alloys
- Interdiffusion in composite materials
  - coating/substrate systems
  - weldments between steels
  - joints of dissimilar steels
- Gradient sintering of cemented carbide work-tool pices

Engström et al, Met Mat Trans A 25A(1994)1127

# Homogenization model

This approach allow us to account for diffusion in more than one phase



Equilibrium calculation  
for each slice

Phase fractions  
Phase compositions  
Chemical potentials  
Mobilities

Flux between slices "n-1" and "n"

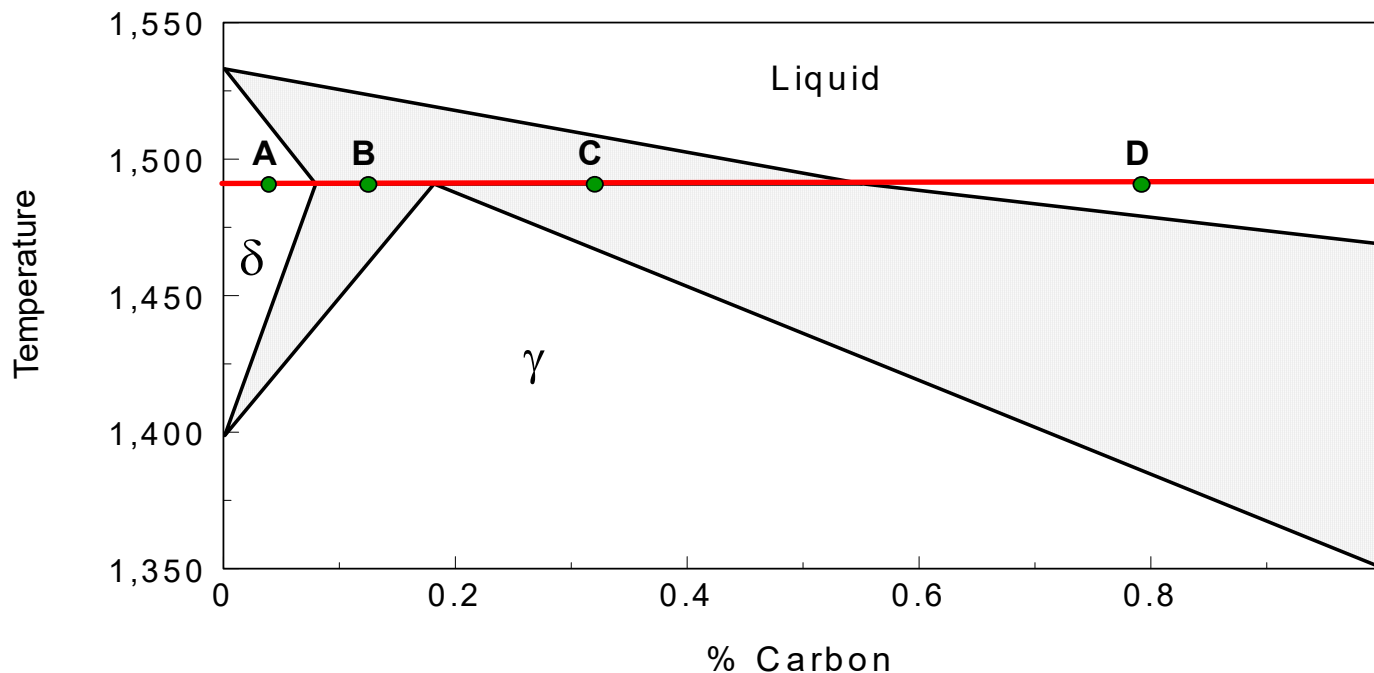
$$J_k = \frac{-1}{V_m} \sqrt{[M_k x_k]_{n-1}^{eff} [M_k x_k]_n^{eff} \frac{\Delta \mu_k}{\Delta z}}$$

"Effective"  $[M_k x_k]$  from combining rules

Larsson, Engström, *Acta Mater* 54(2006)2431  
Larsson, Höglund, *Calphad* 33(2009)495

# Case study: Micro-segregation during solidification

- ❑ VESPIISM (Virtual Experiments to Solve Problems In Steel Metallurgy).
- ❑ Development of phase-field code (MICRESS) linked to Thermo-Calc.
- ❑ Solidification experiments were performed for alloys A – D below as one assignment in this project.

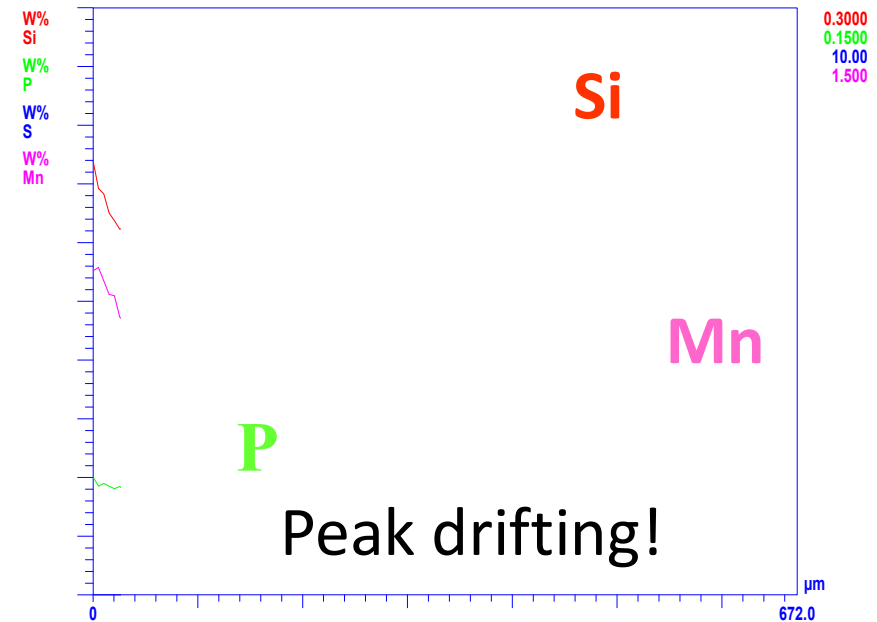
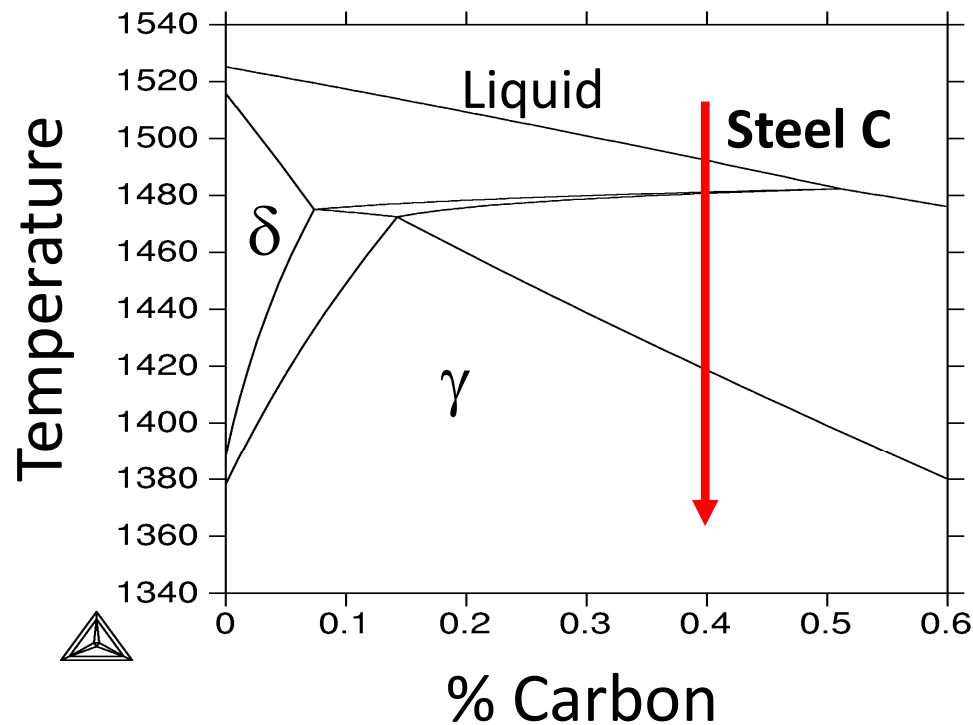


# Observed micro-segregation in Steel C

Steel C:

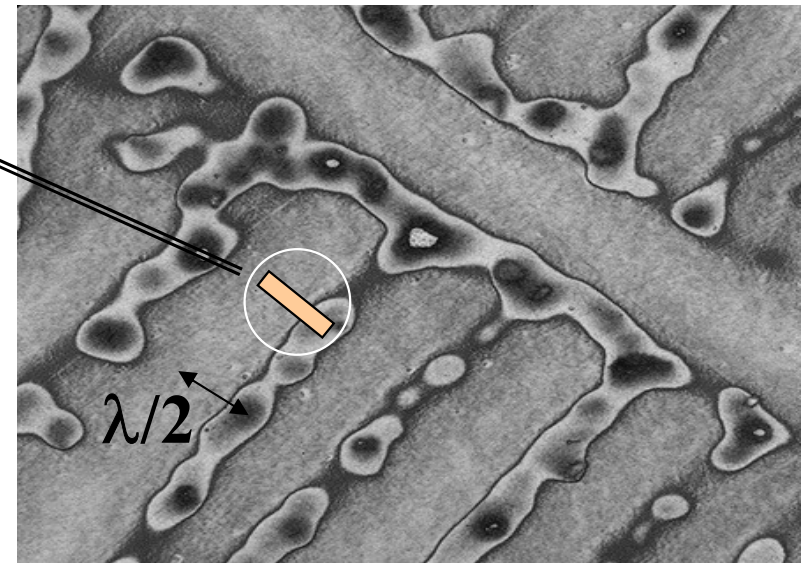
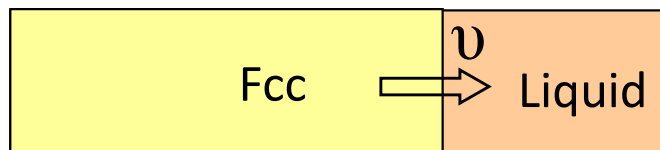
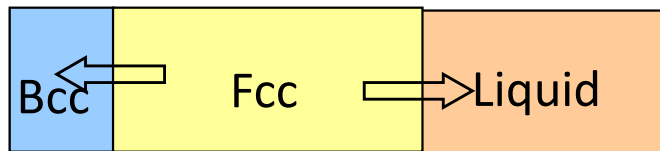
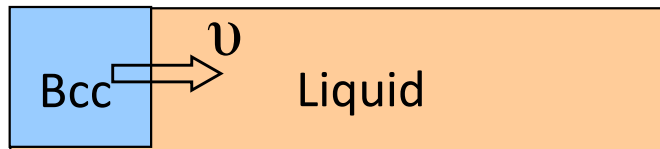
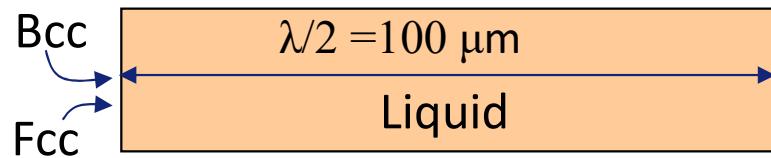
Fe - 0.8% Mn - 0.7% Si - 0.03% P - 0.4% C

*Line-scans across the dendrite arms  
(performed by Corus-UK)*



**Question:** Why does the P peak drift away from the Mn and Si peaks?

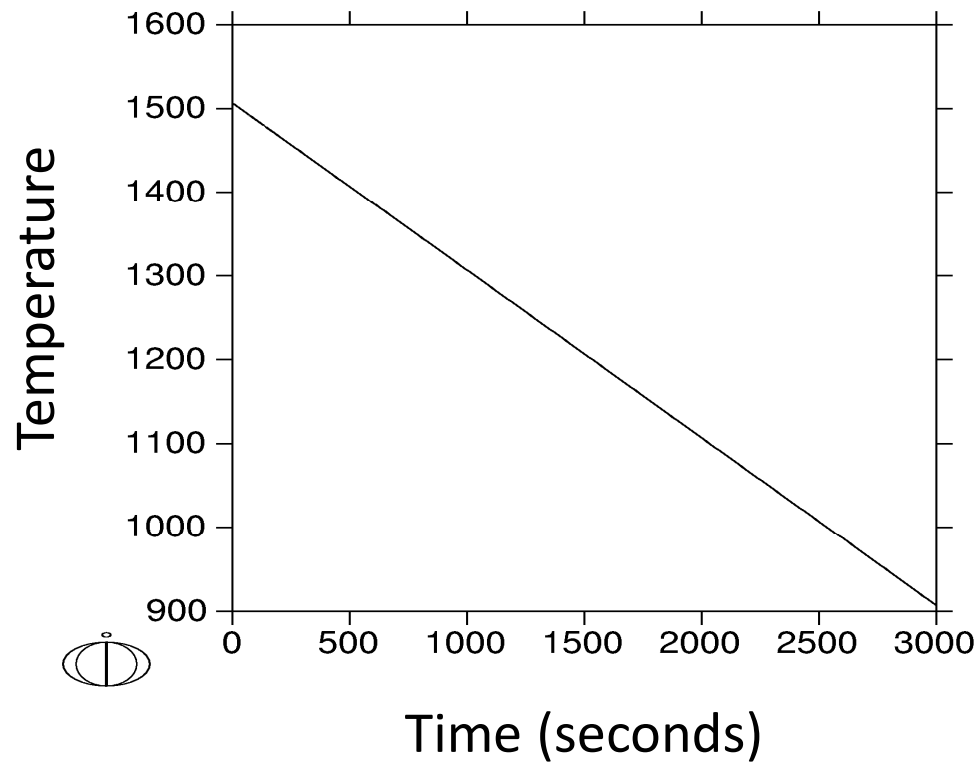
# Analysis using DICTRA



- Secondary dendrite arm spacing assumed to be  $200 \mu\text{m}$ .



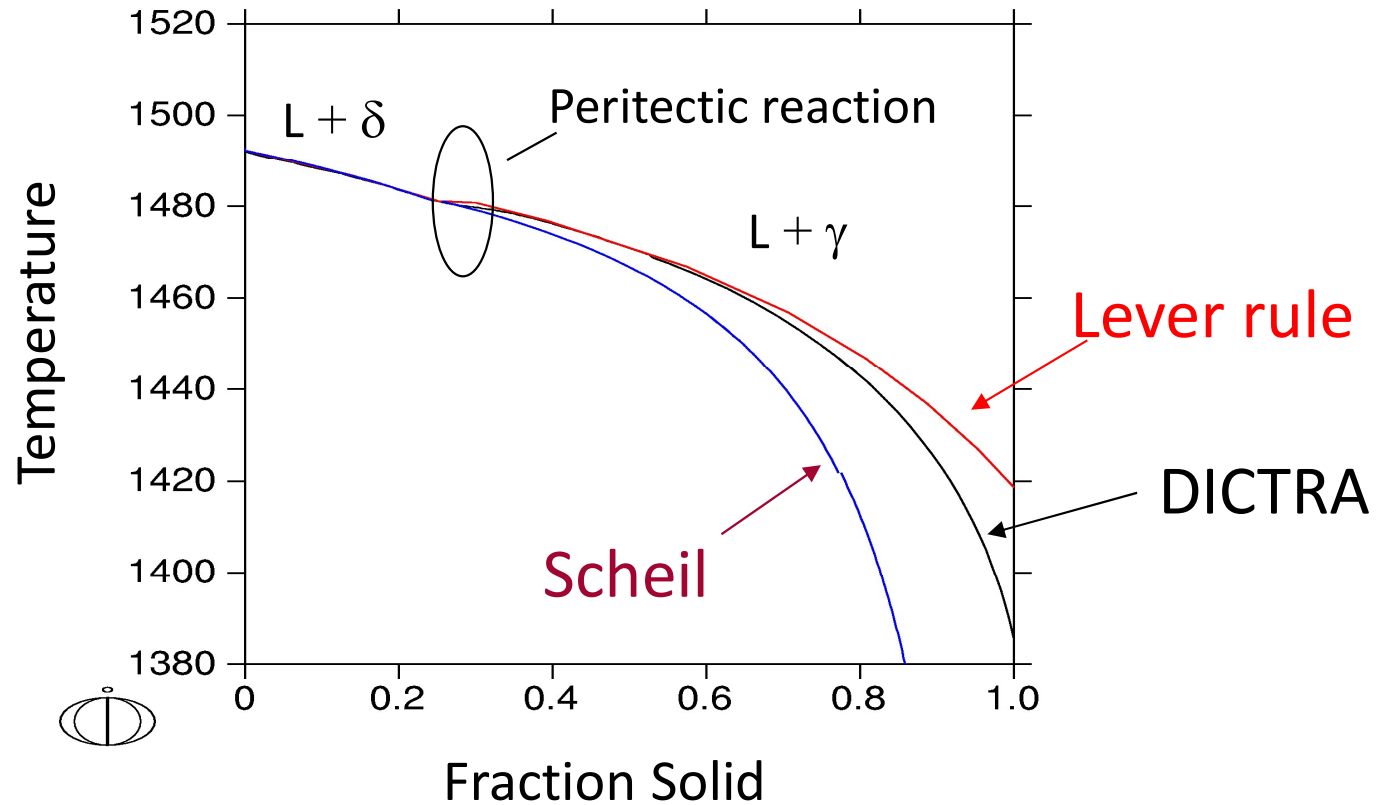
# Cooling function



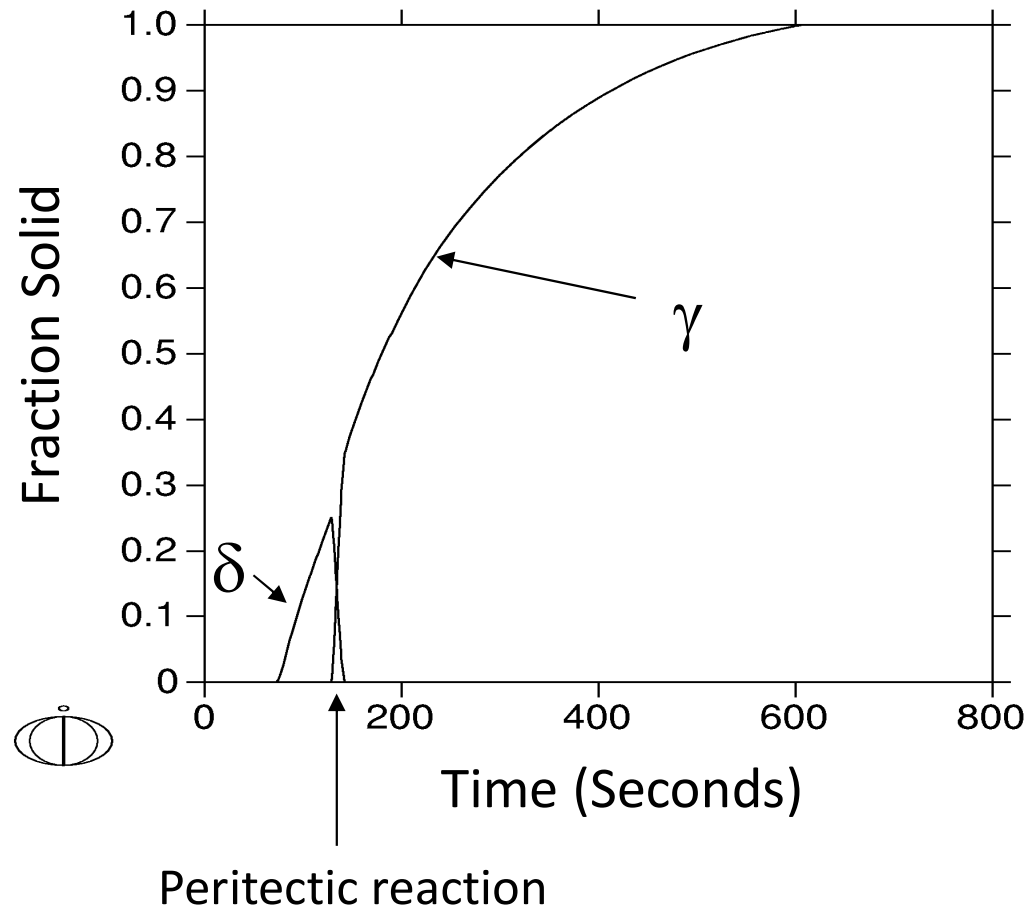
**Cooling rate assumed to be 0.2 °C/s**

- More advanced cooling functions may of course also be imposed.
- Also possible to instead define a condition on the rate of latent heat removal from the system.

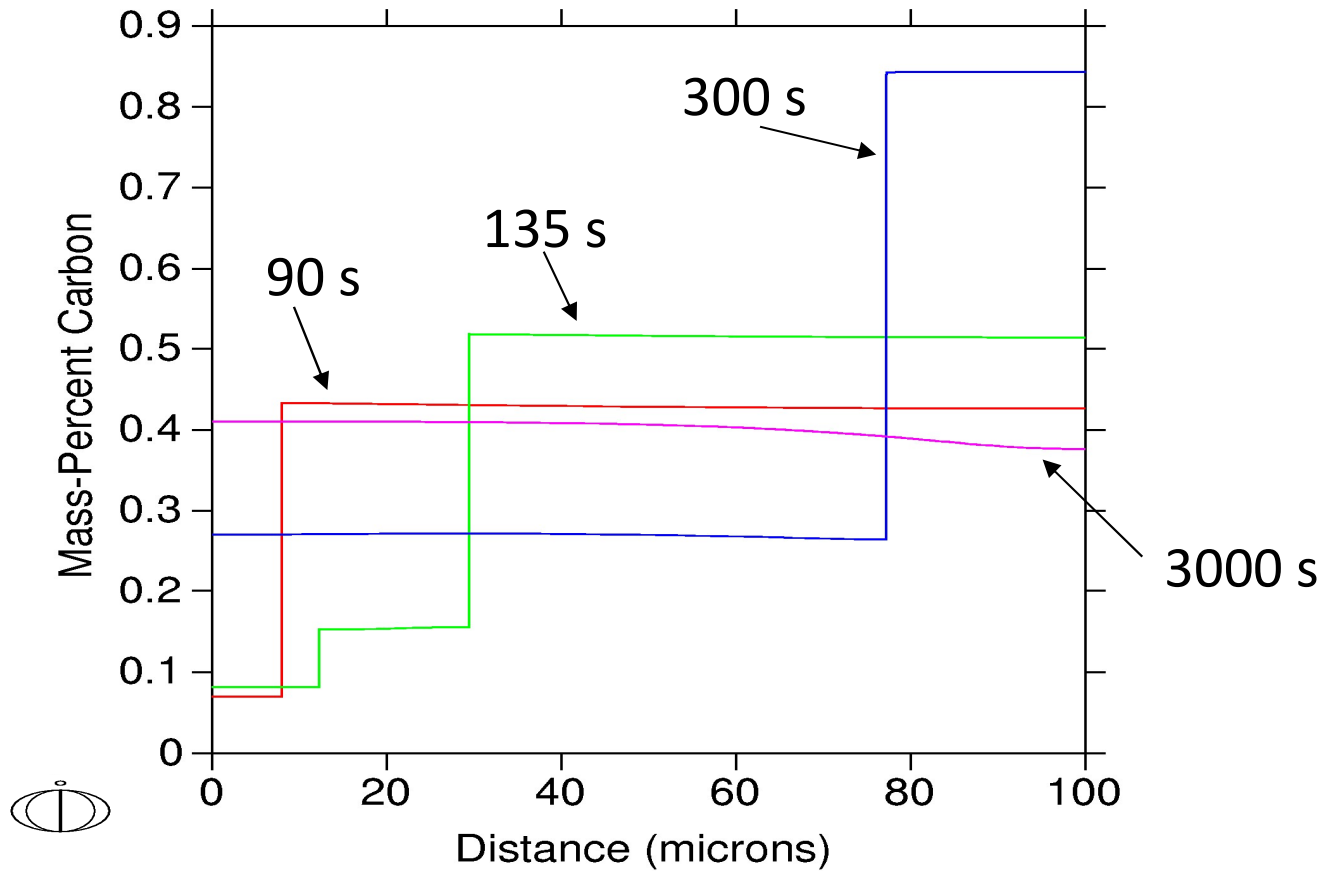
# Solidification range



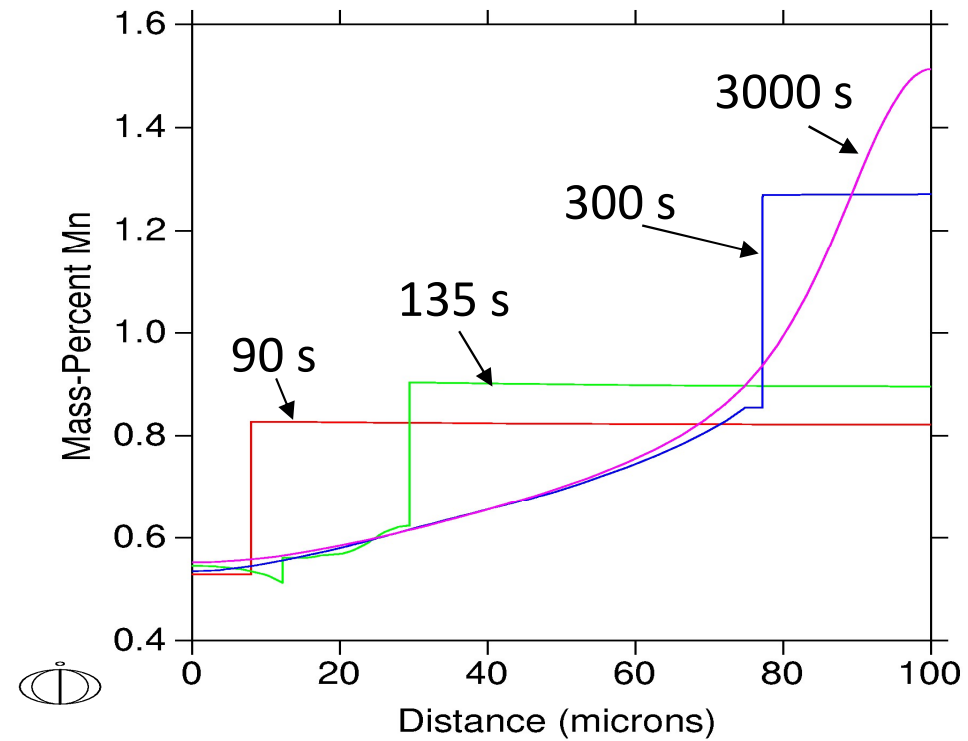
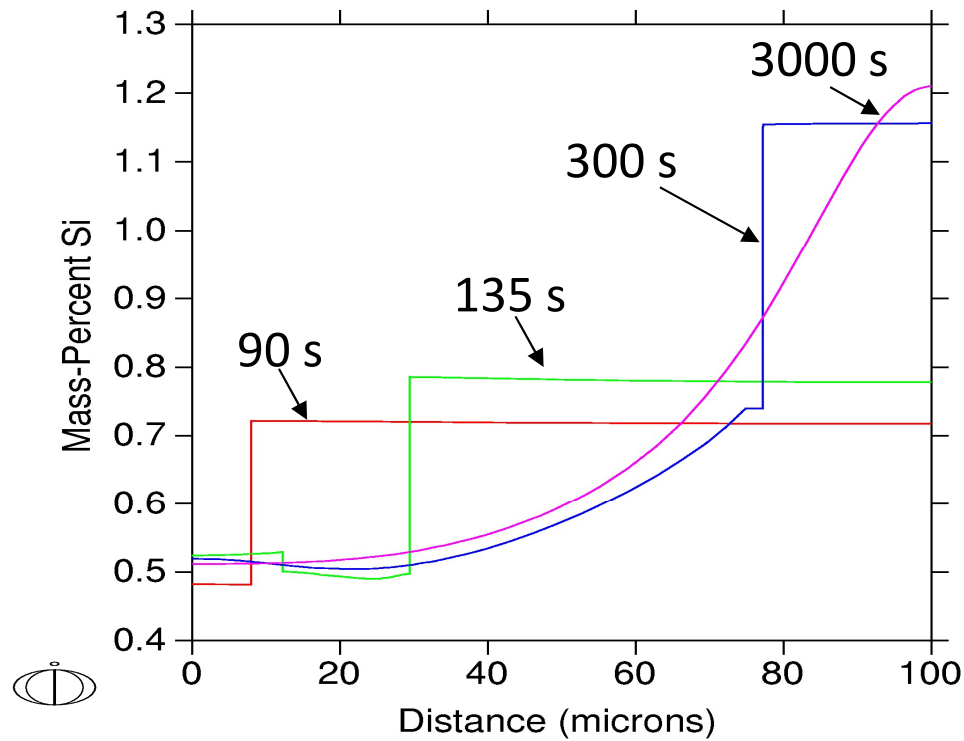
# Fraction of solid phases



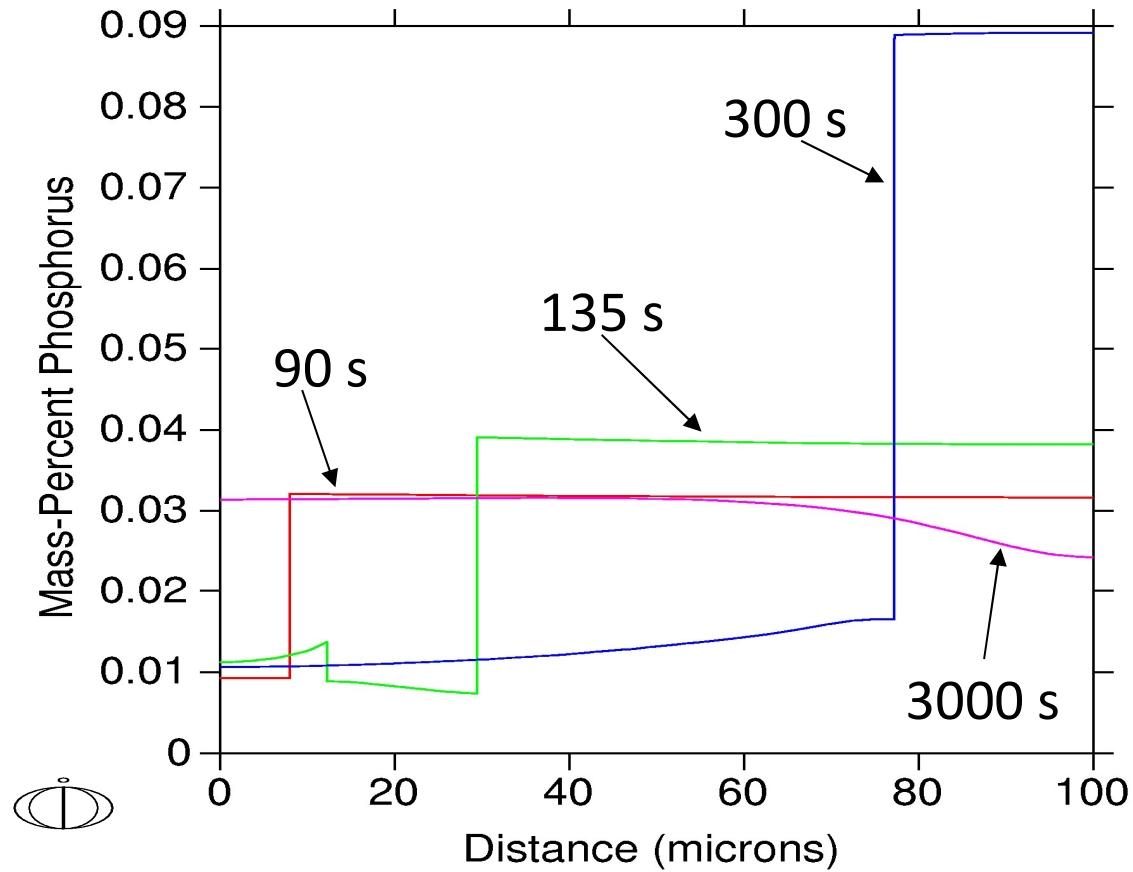
# Carbon profiles during solidification



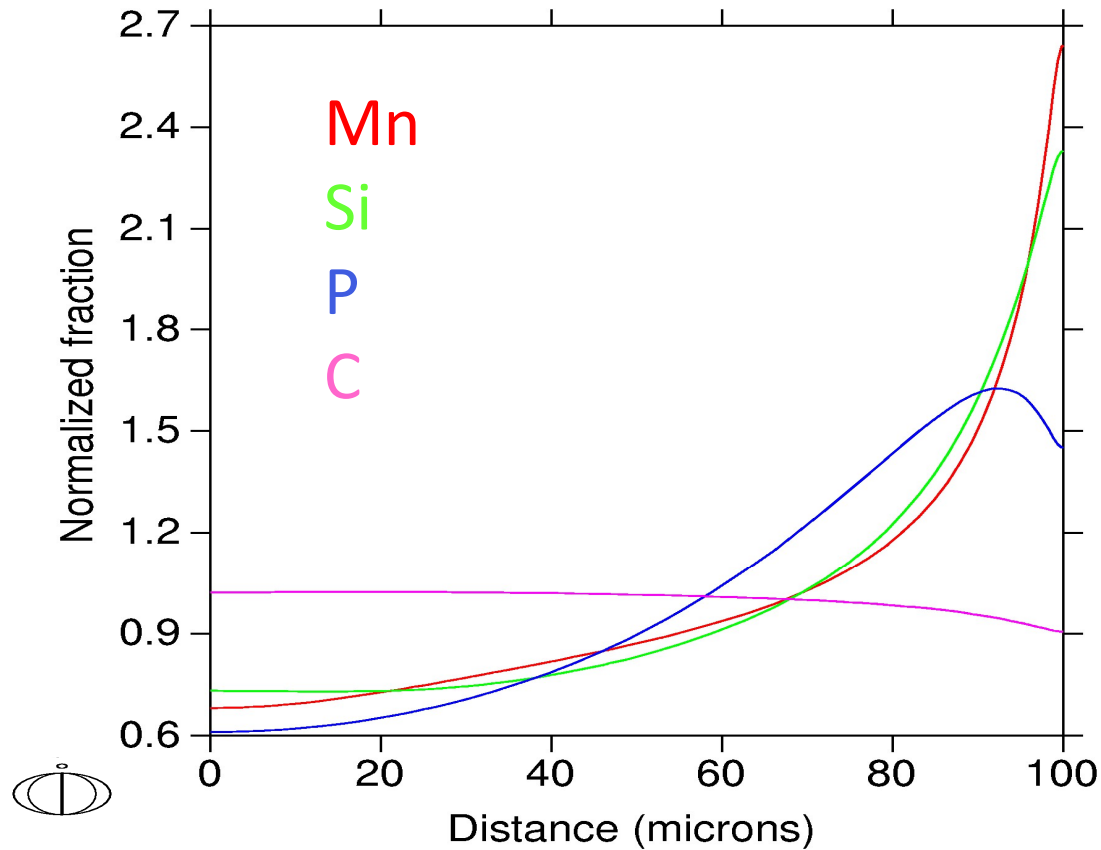
# Silicon and Manganese



# Phosphorus

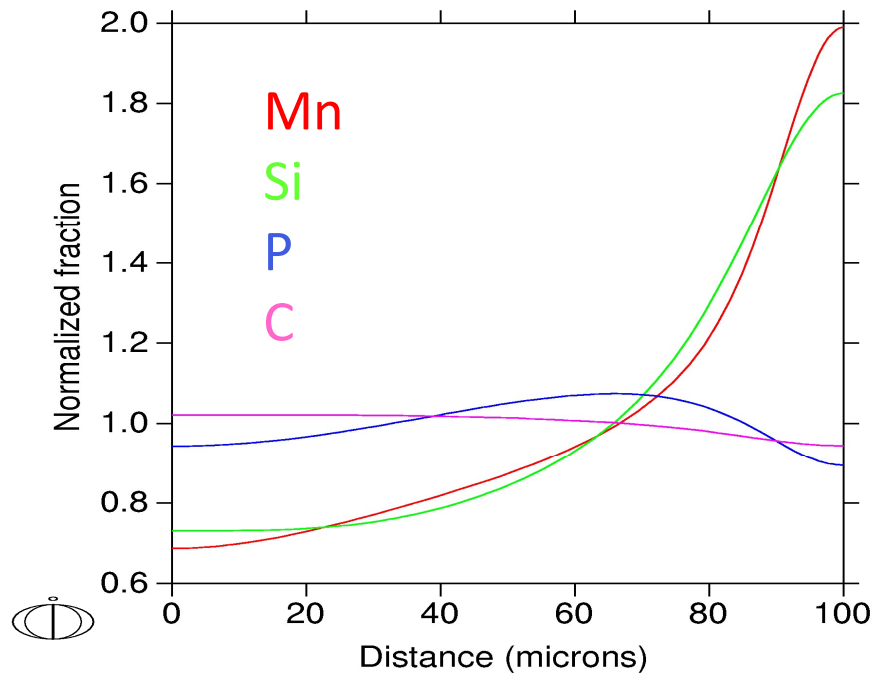


# Segregation profiles after 610 s (when the last melt disappears)

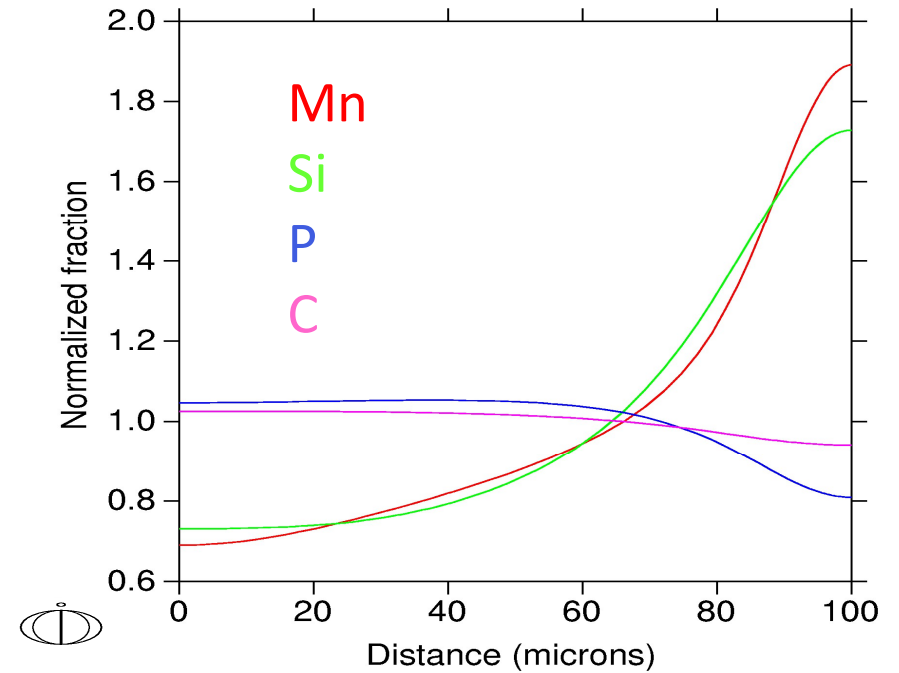


# Segregation profiles after 1000 and 3000 s

after 1000 s

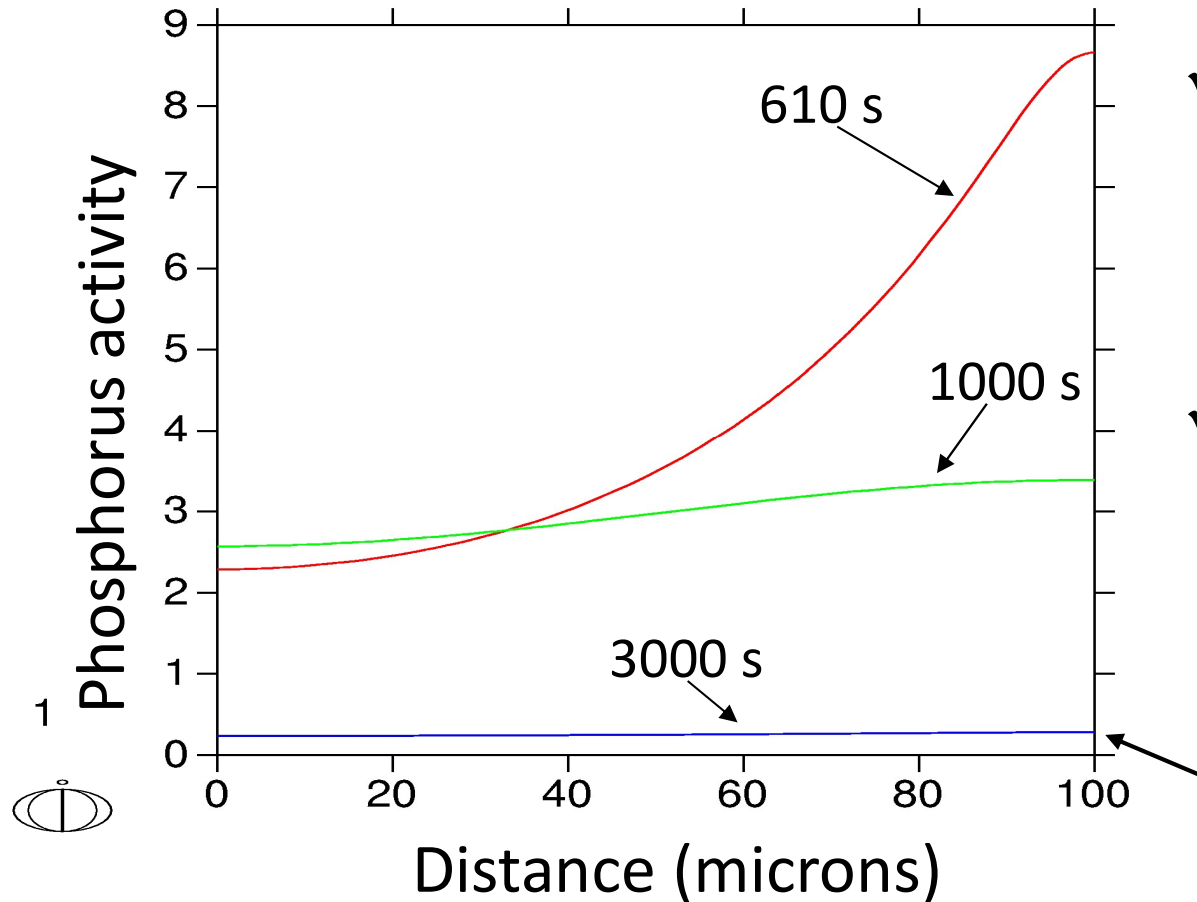


after 3000 s





# The solution



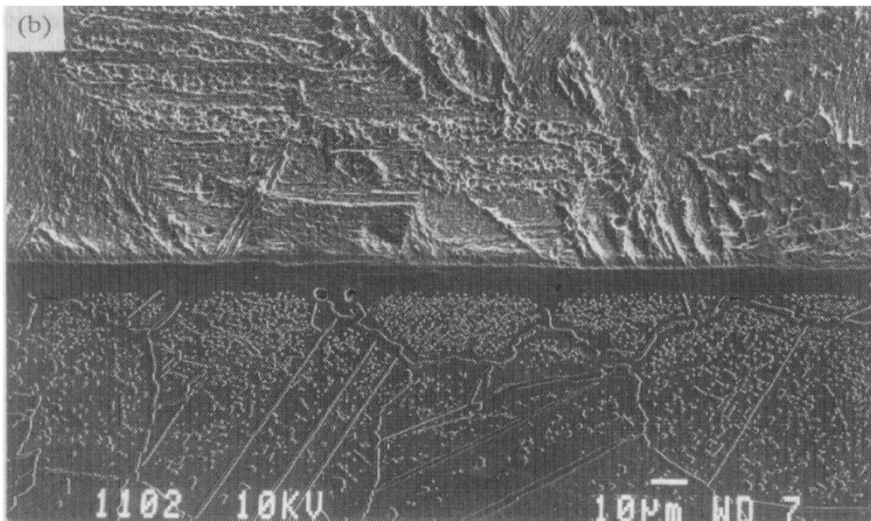
✓ Mn and Si increase the phosphorus activity.

✓ Phosphorus diffusion much faster compared to Mn and Si diffusion.

At the late stage further phosphorus redistribution is controlled by slow Mn and Si diffusion.

# Compound tubes for waste incinerators

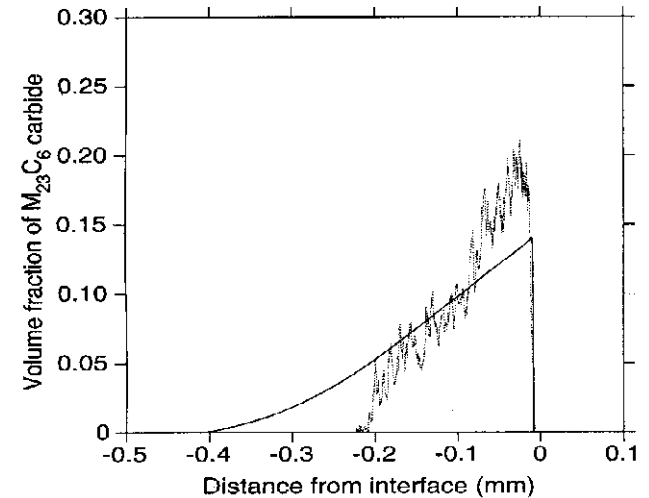
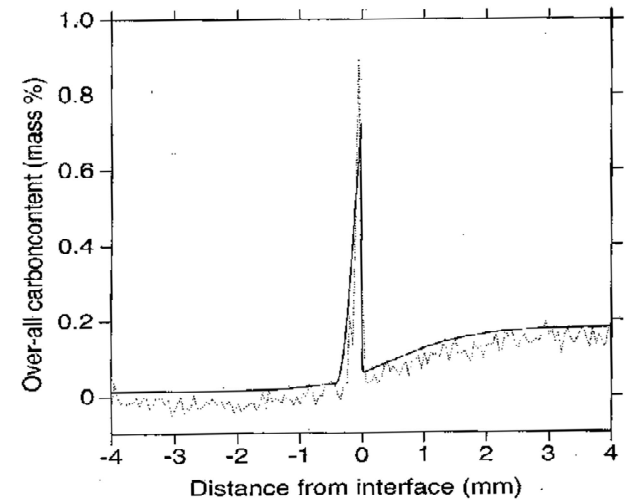
4L7 (0.18% C) After 4 h at 1100 °C



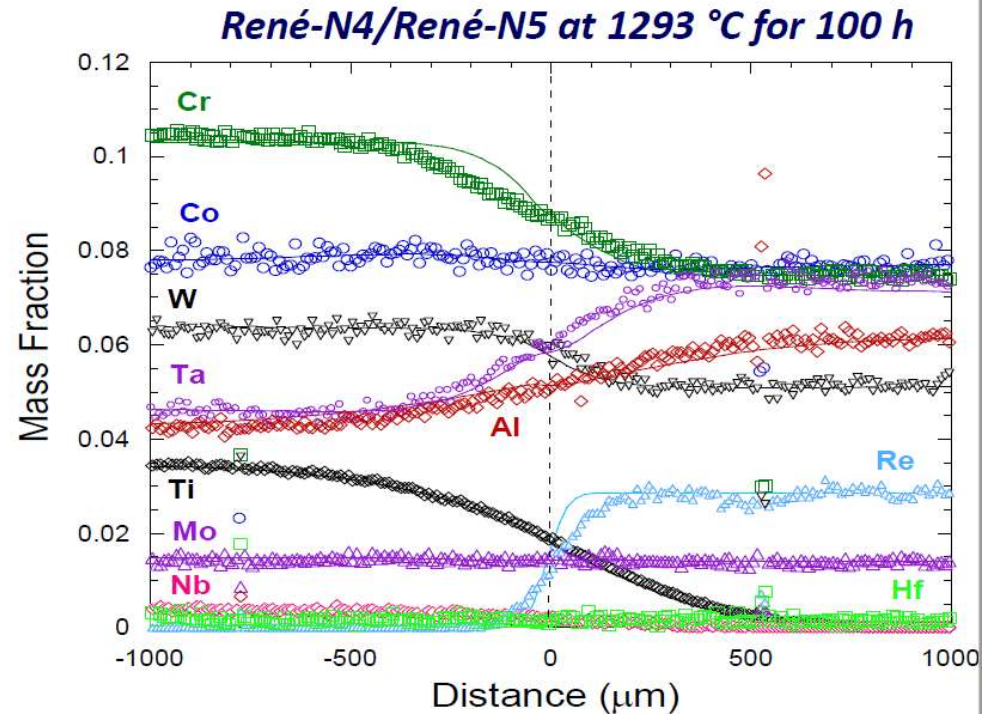
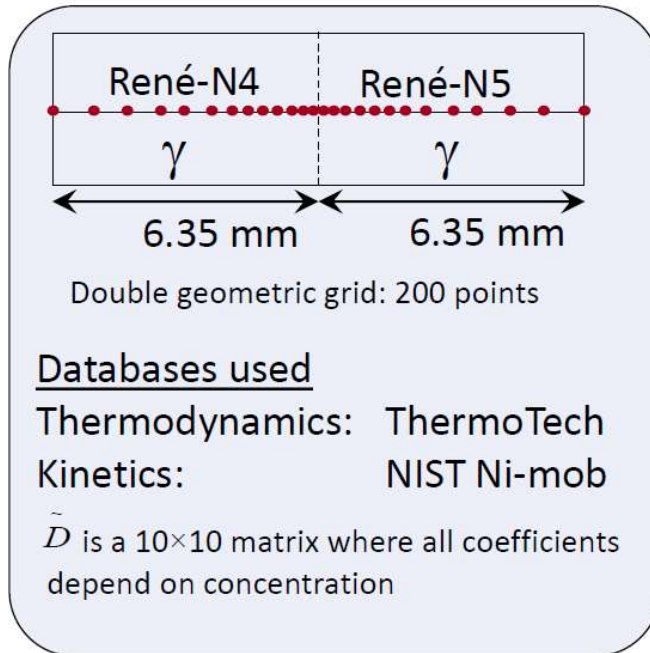
Sanicro28

(30.5% Ni, 27% Cr, 3.3% Mo, 1.8% Mn, 0.014% C)

*Helander, Ågren, Nilsson, ISIJ Int 37(1997)1139*



# Interdiffusion in Ni-superalloys



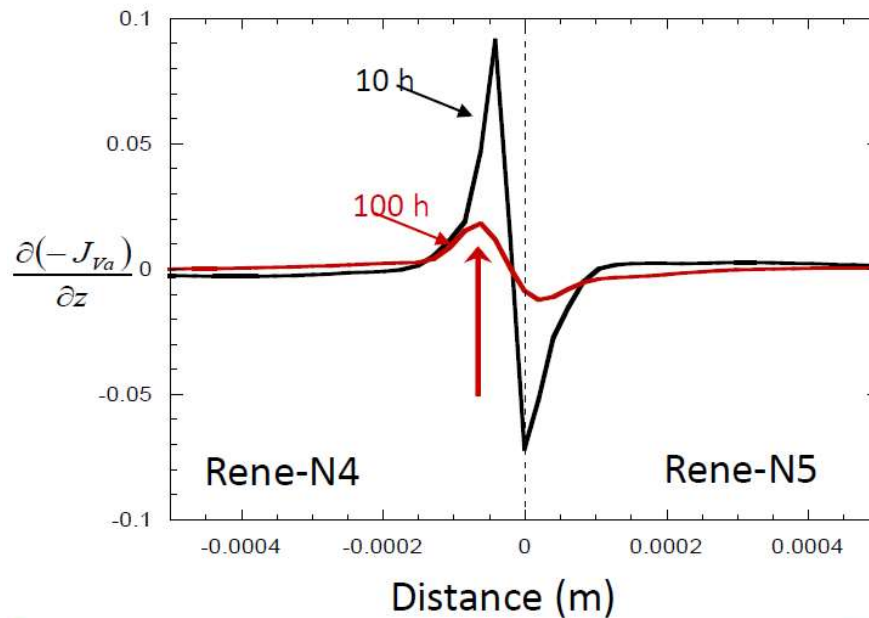
From: C. E. Campbell, Metallurgy Division, NIST

See also: Campbell et al, Mat Sci Eng A 407(2005)135

Experimental work performed by T. Hansen, P. Merewether, B. Mueller, Howmet Corporation, Whitehall, MI.

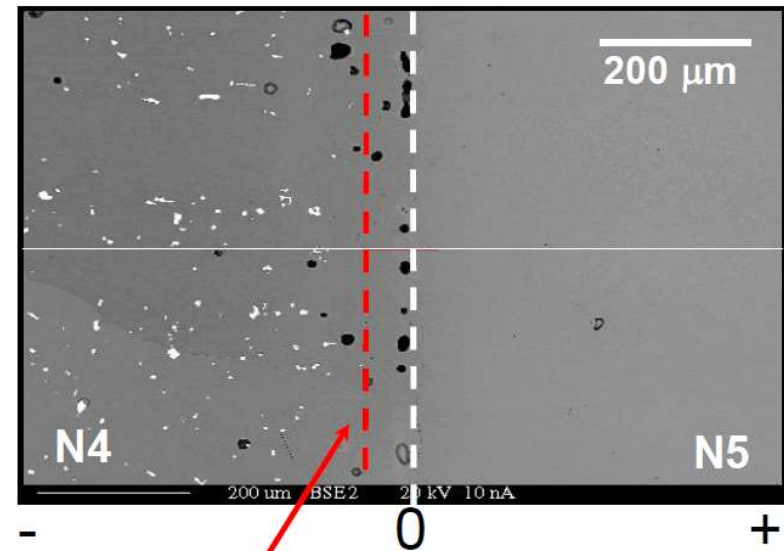
# Interdiffusion in Ni-superalloys

Kirkendall porosity prediction



Maximum gives location of pore formation.

Back scatter image; 100 h



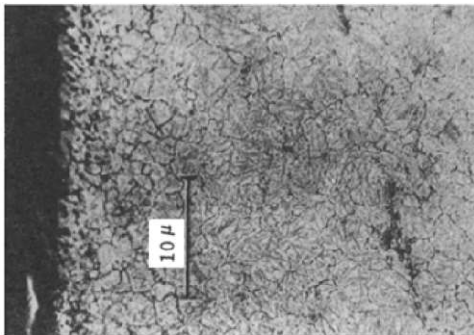
Predicted position for maximum pore formation

From: C. E. Campbell, Metallurgy Division, NIST

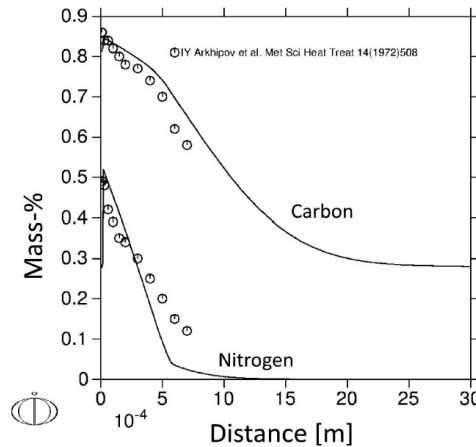
See also: Campbell et al, Mat Sci Eng A 407(2005)135

# Coupled carbonitriding and internal oxidation

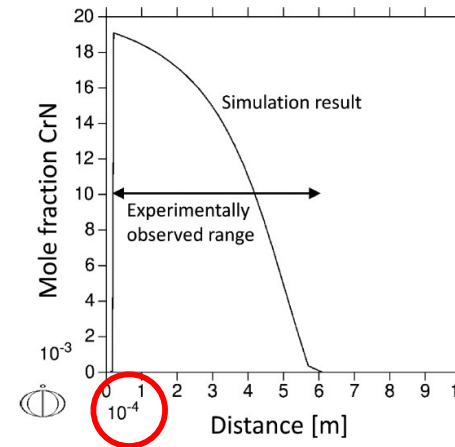
Fe-0.28C-1.15Cr-0.95Mn-0.27Si  
850°C, 24 h



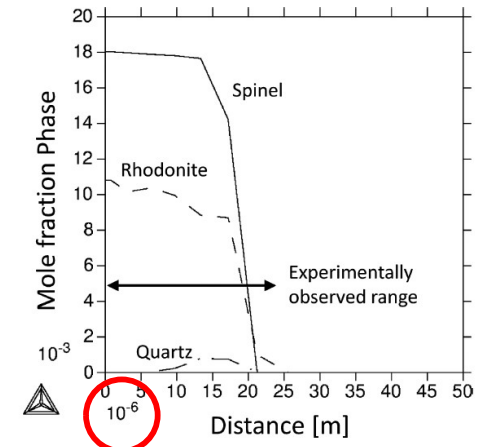
### Concentrations



### Fraction nitride



### Fraction oxides



Micrograph and experimental data  
Arkhipov et al Met Sci Heat Treat 14(1972)508

Larsson, Ågren, HTM J Heat Treatm Mat 72(2017)19



# Compatibility of Databases



Thermodynamic Database	Kinetic Database
SSOL2, SSOL4, SSOL5, SSOL6, SSOL7, SSOL8	MOB2
TCFE5 and earlier versions	MOB2
TCHEA2, TCHEA3+4+5, TCHEA6+7	MOBHEA1, MOBHEA2, MOBHEA3
TCFE6, 7, 8, TCFE9, TCFE10, TCFE11, TCFE12, TCFE13	MOBFE1, 2, 3, 4, 5, 6, 7, MOBFE8
TTNI8 and earlier versions	MOBNI1
TCNI4, TCNI5, TCNI6*	MOBNI2*
TCNI7, TCNI8	MOBNI3, MOBNI4
TCNI9+TCNI10+TCNI11, TCNI12	MOBNI5, MOBNI6
TTAL8 and earlier versions	MOBAL1 and BISHOP
TCTI4, TCTI5	MOBTI4
TCAL1+2+3, TCAL4,TCAL5, TCAL6+7, TCAL8, TCAL9	MOBAL3,4,5, MOBAL6, MOBAL7, MOBAL8
TCMG1+2+3+TCMG4+TCMG5, TCMG6	MOBMG1, MOBMG2
TCCU1, TCCU2, TCCU3, TCCU4, TCCU5 + TCCU6	MOBCU1, 2, 3, 4, MOBCU5

\* Pairing of TCNI6 and MOBNI2 is not possible for the LIQUID phase.

# Some DICTRA specific concepts.

Terminology needed mostly for Console Mode

# Region

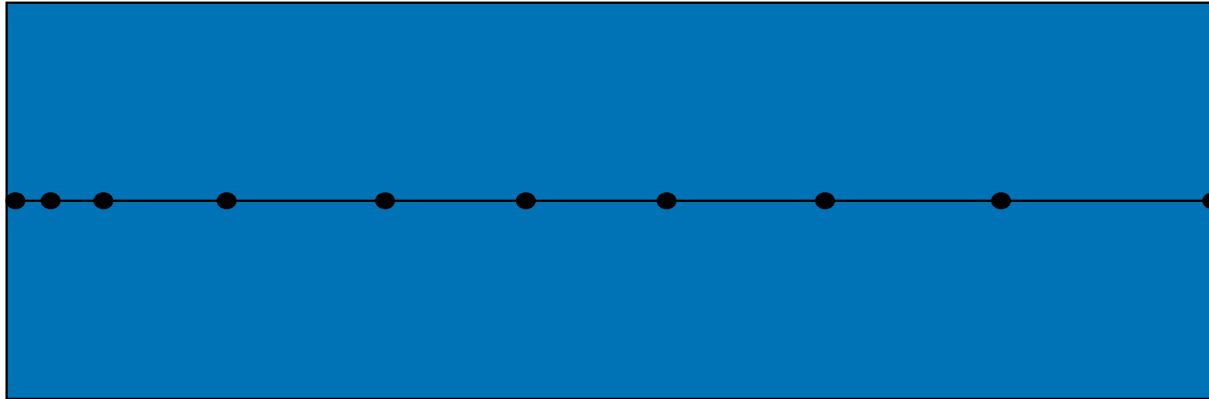


A "box" filled with the phase(s) where diffusion takes place. Can be given any name.

The region has two boundaries, left and right.

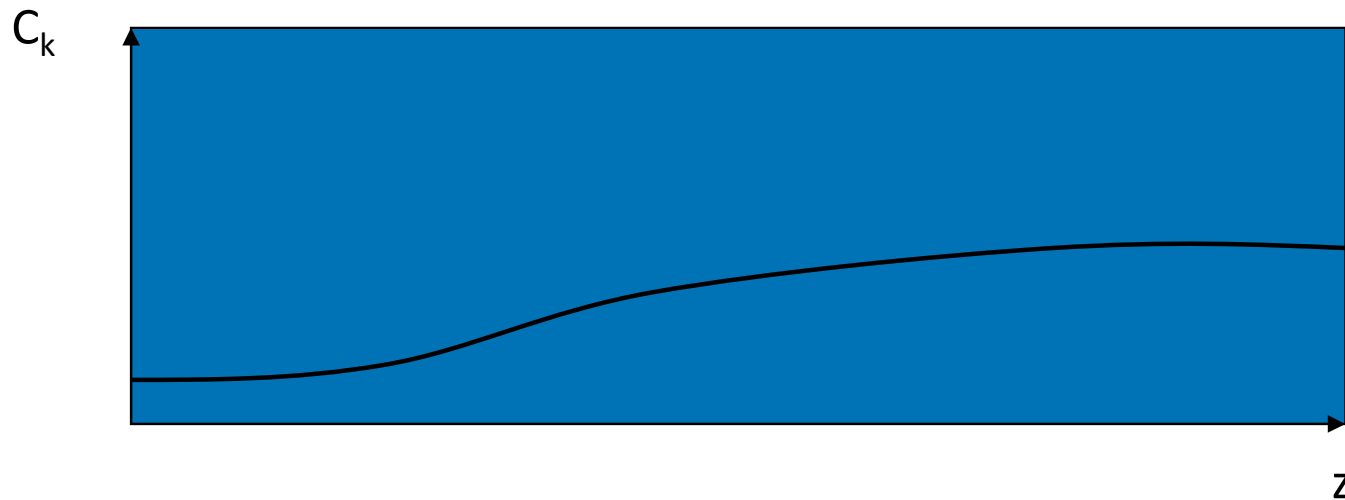


# Grid



Distribution of node points for numerical calculations (inside the region).

# Concentration Profile



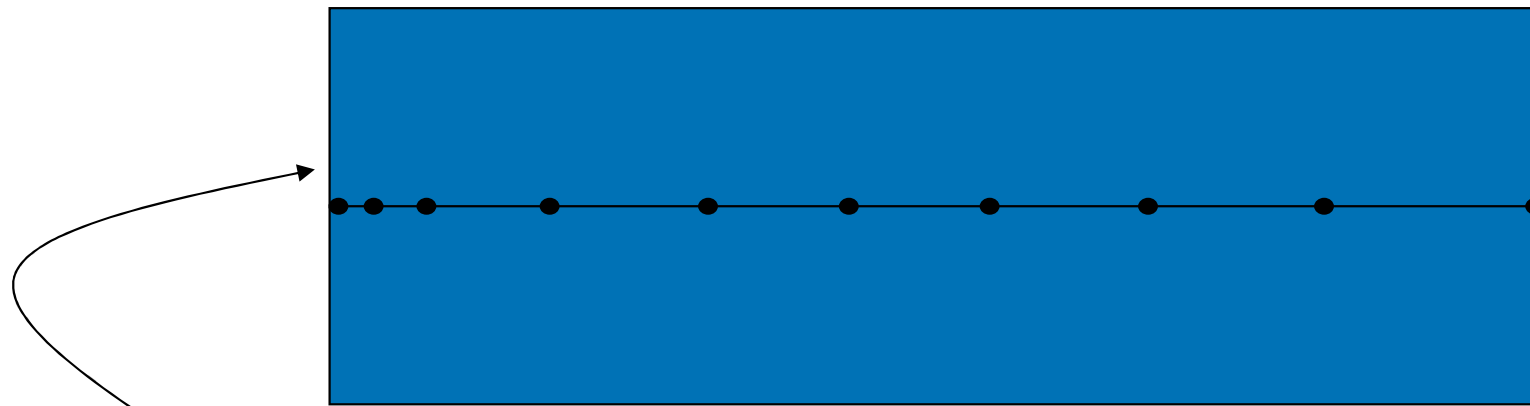
Concentration,  $C_k$  of an element as a function of distance  $z$ .

# Global Conditions



Conditions valid for entire system, T and P.

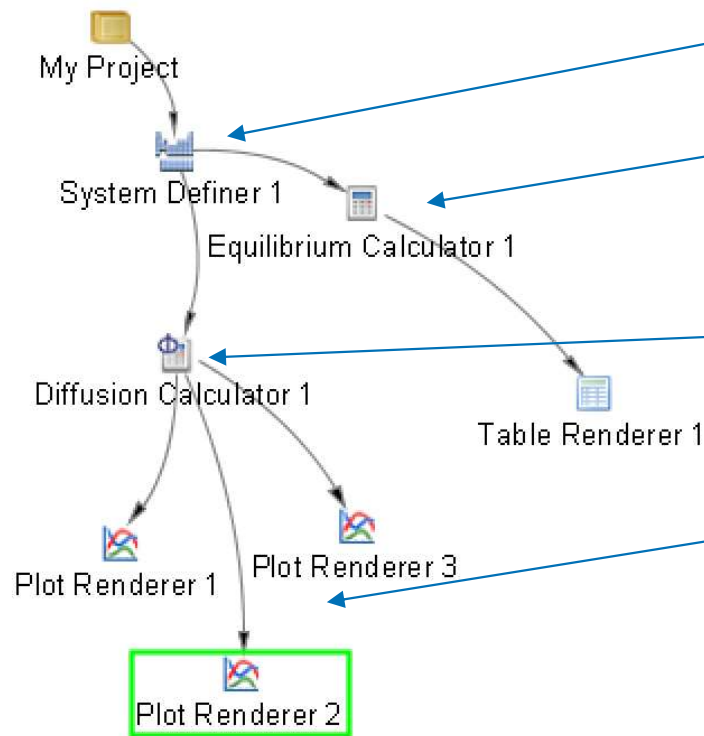
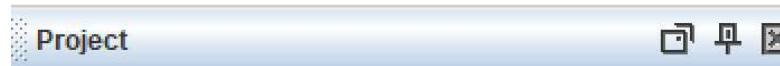
# Boundary Conditions



$a_c=1$  (carburization)

Conditions that apply to region boundaries (can be functions of time and temperature).

# DICTRA Project in Graphical mode



Thermodynamic + Mobility data!

Preliminary Thermo-Calc calculation.  
(not included in template)

Diffusion simulation setup & run.

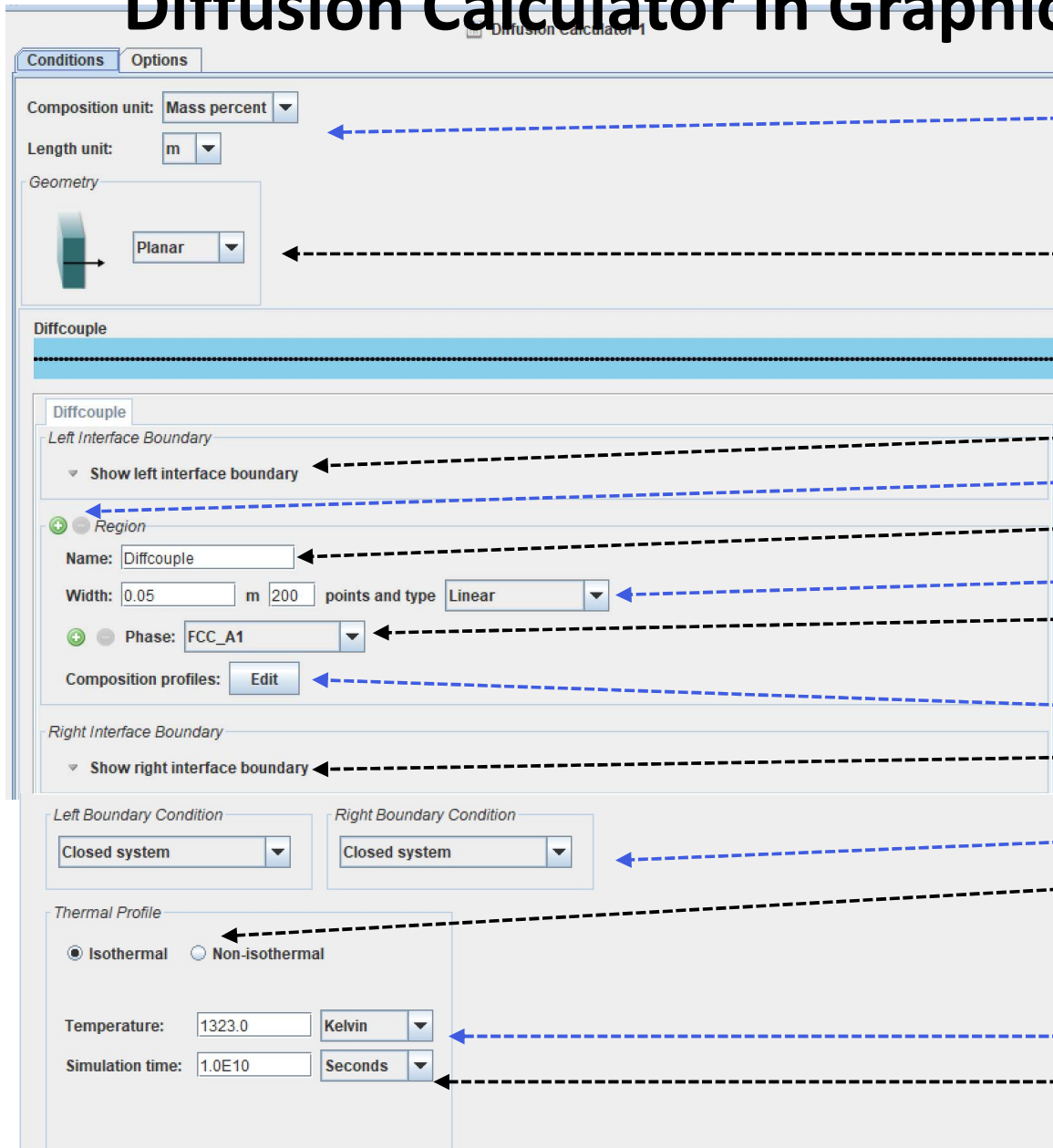
Typically many different plots from a  
single simulation (only 1 in template).

# Typical calculation setup - Graphical



1. Select thermodynamic and kinetic data
2. Choose units for composition and distance
3. Enter geometry
4. Enter region(s)
5. Enter grid(s) in region(s)
6. Enter phase(s) in region(s)
7. Enter composition(s) for the phases
- (8. Set boundary conditions)
9. Set condition for temperature
10. Set simulation time
11. Perform simulation

# Diffusion Calculator in Graphical mode



Set composition unit & length unit

Set geometry

Visual of the region with its grid.

Click to set phase to form on the left.

Click plus to add more regions.

Name the predefined 1<sup>st</sup> region.

Set region size, grid points and type.

Set matrix phase in region. Click plus to add more phases.

Set the composition for matrix phase.

Click to set phase to form on the right.

Set boundary conditions.

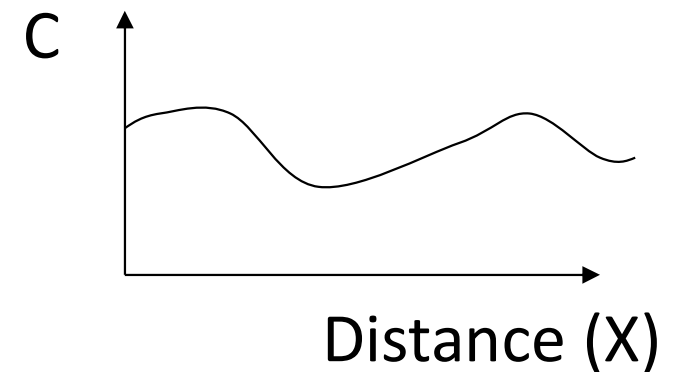
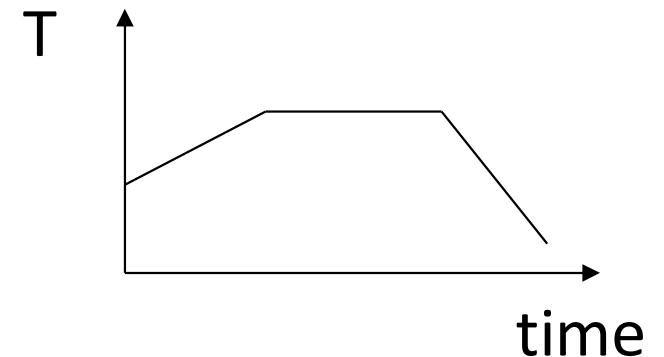
Select isothermal or not. If not, a box for editing T-profile will open.

Set iso-thermal temperature.

Set simulation time.

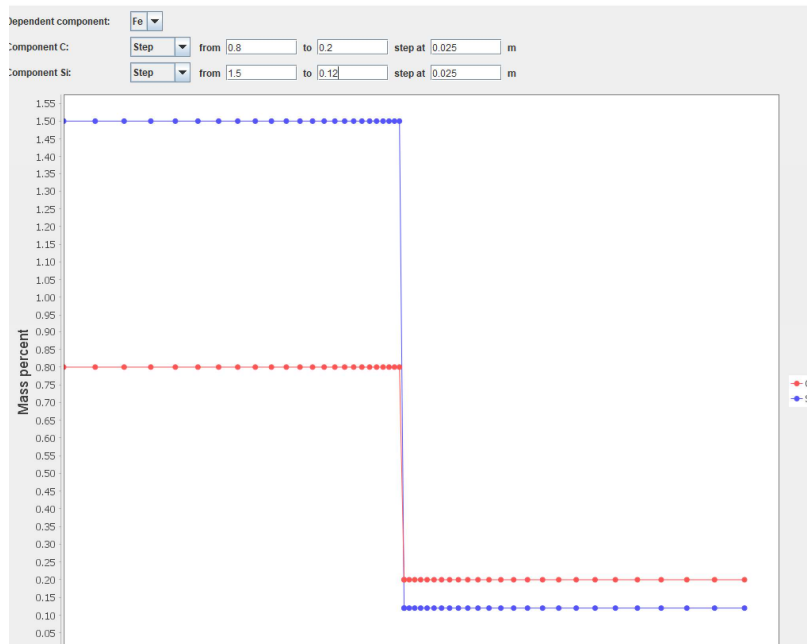
# Input of T and c – Console mode

- ❑ Temperature (T) can be entered as a function of time (and distance)
- ❑ Many different functions can be used (+, -, \*, \*\*, SQRT(X), EXP(X), LOG(X), SIN(X))
- ❑ Initial concentration can be entered as a function of distance or read from a file
- ❑ Special functions e.g. error-functions (erf(x)) and heaviside step functions (hs(x)) can be used.



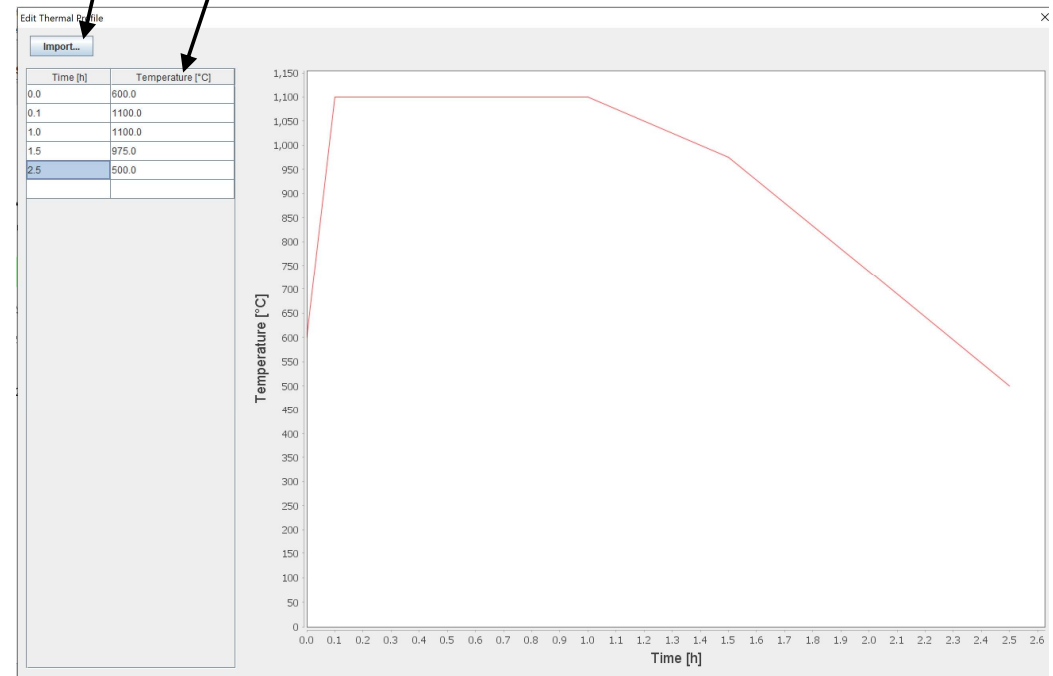


# Input of c and T – Graphical mode



Input of Temperature profile:  
- isothermal  
- import from file (e.g. Excel)  
- edit by hand

Input of composition profile:  
- Linear  
- Step (shown above)  
- Function



# One phase Example

## - Uphill diffusion

# Uphill diffusion in a Fe-Si-C alloy

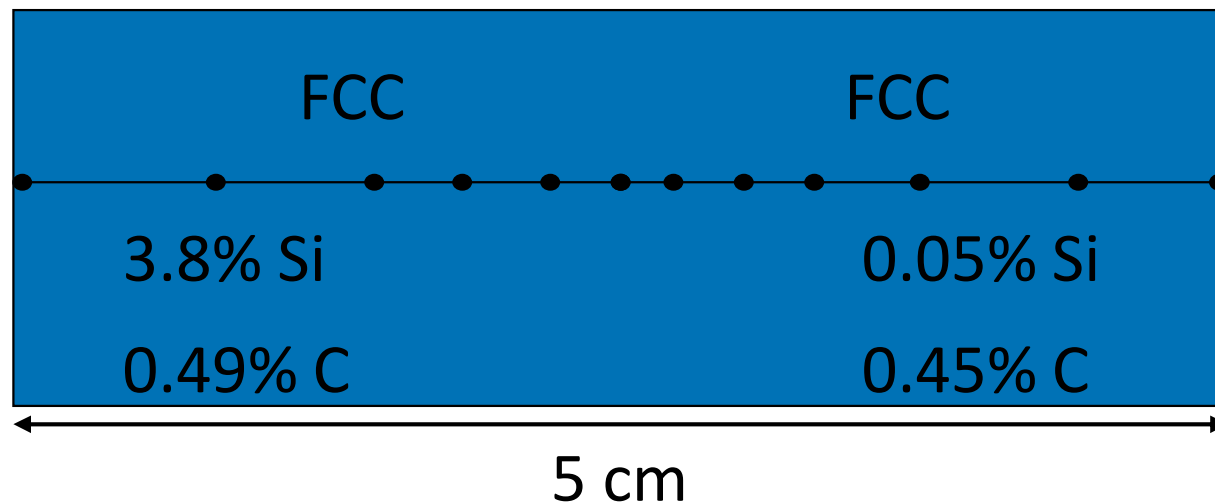
- In a classic experiment (published 1949), L.S. Darken welded together two steels having similar C-contents, but with different Si-contents.

<u>Steel 1</u>	<u>Steel 2</u>
3.8 %Si	0.05 %Si
0.49 %C	0.45 %C

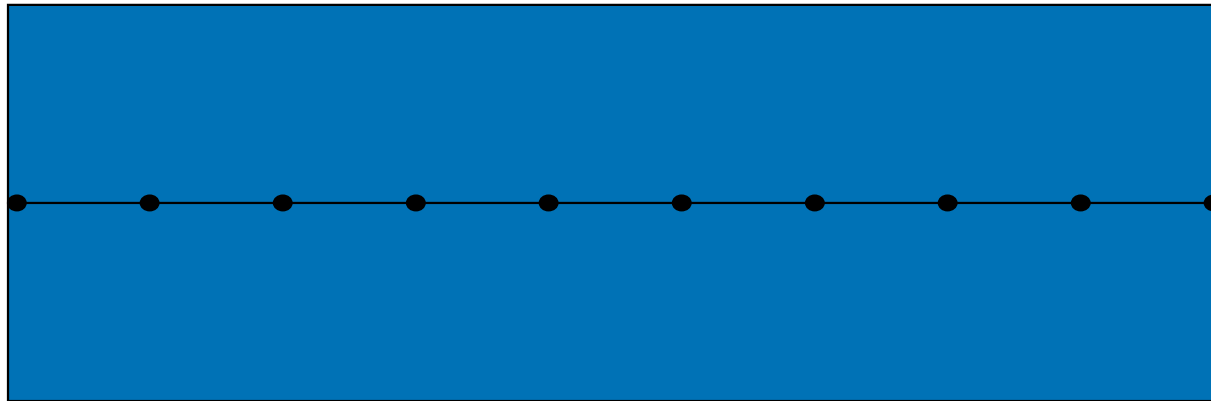
- After annealing Darken was able to conclude that C had diffused up its own concentration gradient, so-called “uphill diffusion”. Darken thereby proved that it is the difference in C-activity rather than the difference in C-concentration that is the driving force for diffusion.

# DICTRA Setup

- One single region entered.
- Only FCC entered into this region, i.e. single-phase.
- Composition profiles entered with a step in center.
- Closer spacing between grid points towards the center.
- Global conditions: Constant temperature,  $T=1050$  C.
- Boundary conditions: Zero-flux (= closed system).

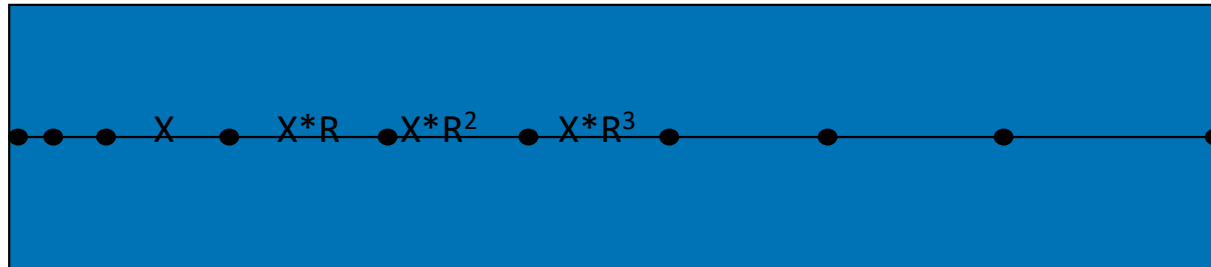


# Linear grid

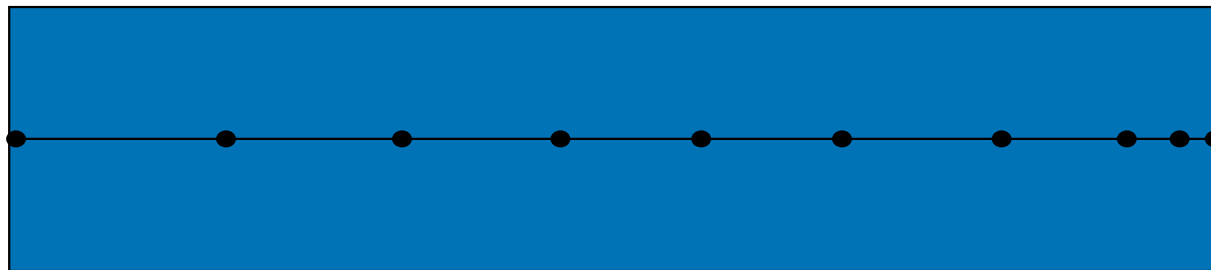


Equidistant distribution of node points.

# Geometric Grid



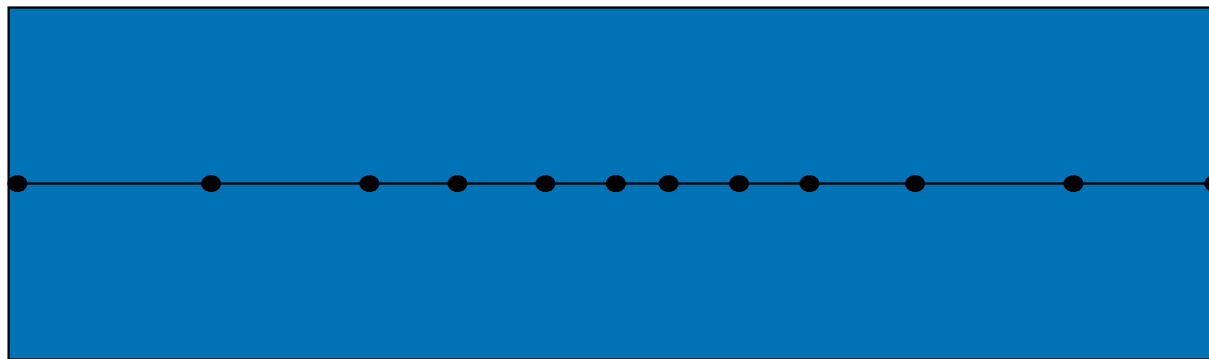
$R > 1$



$R < 1$

Node points represents geometric series

# Double Geometric Grid



$R < 1$

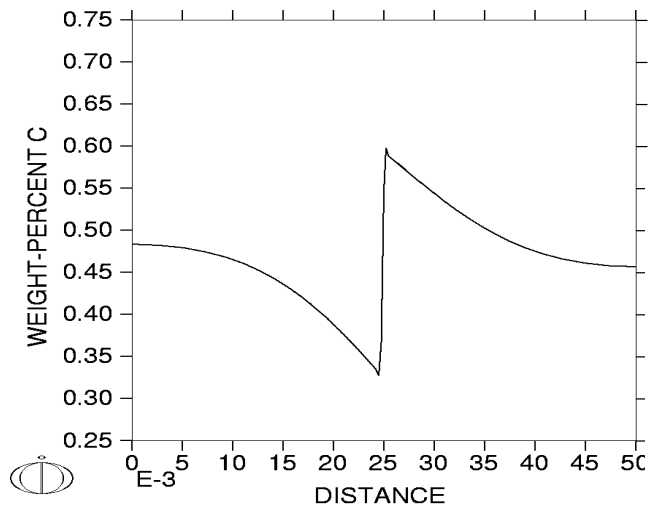
$R > 1$

# Uphill diffusion

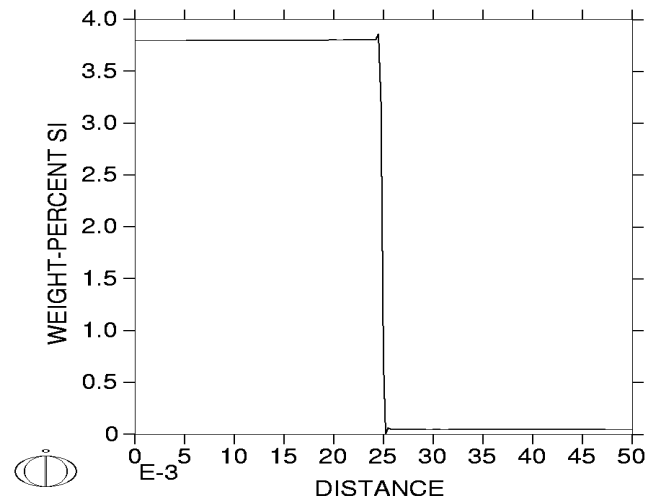
$$J_k = - \sum_{j=1}^{n-1} D_{kj}^n \frac{\partial c_j}{\partial z} \Rightarrow J_C = -D_{CC}^{Fe} \frac{\partial c_C}{\partial z} - D_{C_{Si}}^{Fe} \frac{\partial c_{Si}}{\partial z}$$

"Off-diagonal" term  
Can cause uphill diffusion

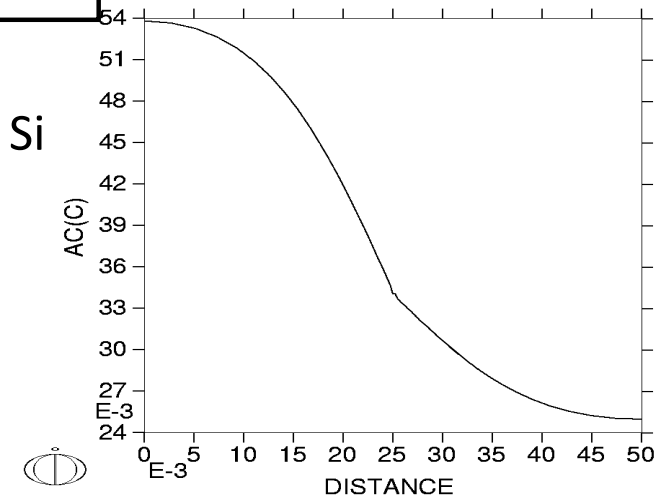
Concentration-profile for C



Concentration-profile for Si



Activity-profile for C



Darken, Trans AIME 180(1949)430



# Uphill diffusion

$$J_C = - \overbrace{D_{Cc}^{Fe} \frac{\partial c_C}{\partial z}}^{\text{Diagonal term.}} - \overbrace{D_{CSi}^{Fe} \frac{\partial c_{Si}}{\partial z}}^{\text{Off-diagonal term.}}$$

Flux of carbon.

Diffusivity of C with respect to the gradient in C. Fe = ref. element.

Conc. gradient for C.

Diffusivity of C with respect to the gradient in Si. Fe = ref. element.

Conc. gradient for Si.

# Q & A

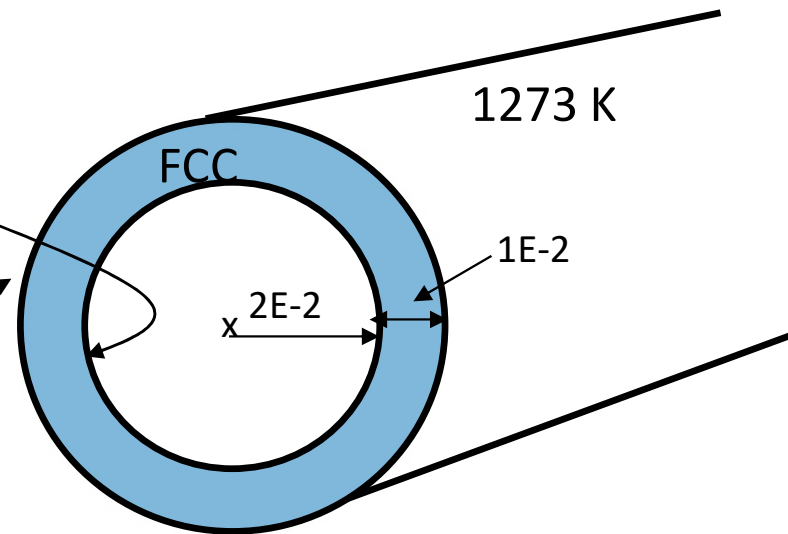
# One phase Example - Carburisation

# Example – diffusion through a tube wall

Boundary conditions:

$$\text{ACR}(C) = 0.9$$

$$\text{ACR}(C) = 0.00001$$



Demonstrates the use of:

- Geometries
- Boundary conditions
- Reference states

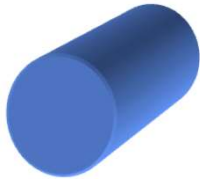
Alloy composition:

Fe – 0.6Mn – 0.7Si – 0.05C (wt-%)

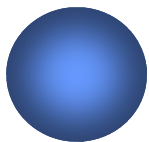
# DICTRA Geometries



Infinitely wide plate of a certain thickness.



Infinitely long cylinder of a certain radius.



Sphere with a certain radius.

# Boundary conditions

In Graphical Mode:

**Closed System** (this is default)

**Mixed zero flux and activity** (Very useful!)

**Composition**

There are some more possible boundary conditions in Console Mode:

**Fix flux value** (very theoretical)

**Potential/Activity flux function** (for real specialists)

**Iterative activity flux function** (for real specialists)

**Gas** (allows for growing/shrinking region)

# U-fraction

The composition variable used internally in DICTRA

”Mole fraction with respect to substitutional elements only”

Natural choice if it is assumed that

- The partial molar volume is the same for all substitutional elements ( $V_S$ )
- The partial molar volume is zero for all interstitial elements

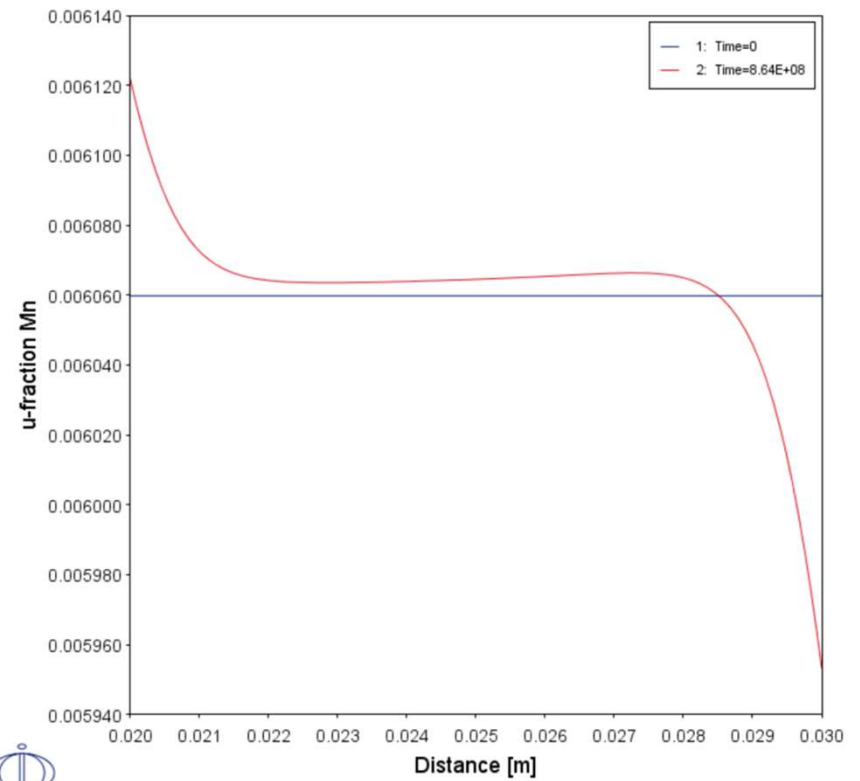
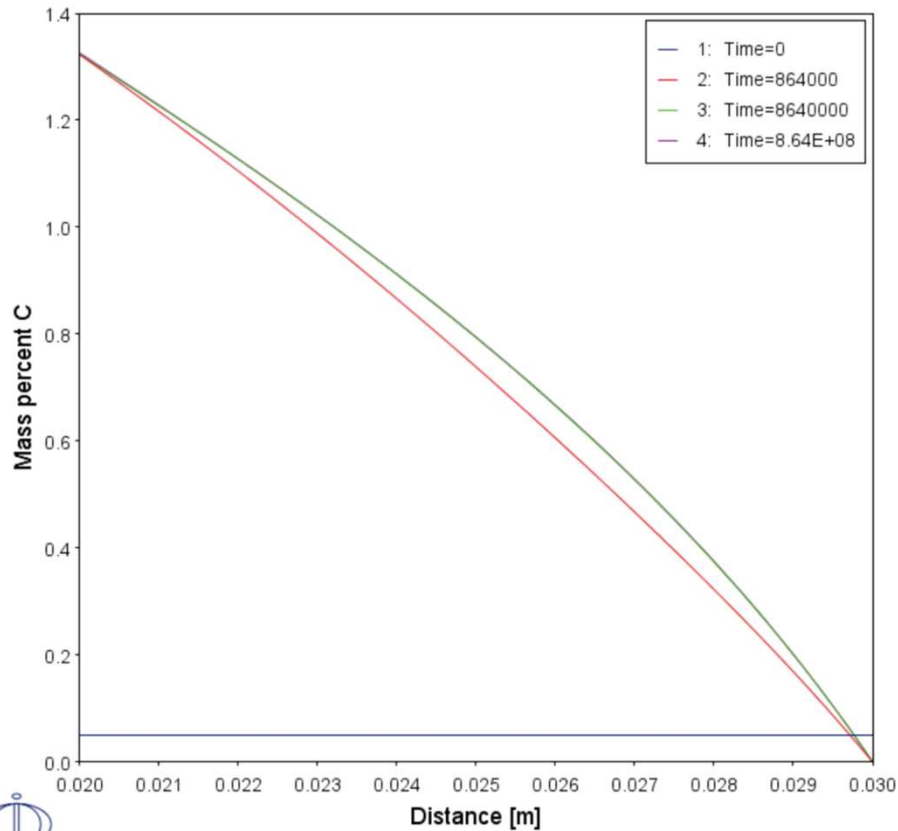
Example: System Fe-Cr-C,  $u_k$  is u-fraction,  $x_k$  is mole fraction

$$u_{Cr} = \frac{x_{Cr}}{x_{Cr} + x_{Fe}} = \frac{x_{Cr}}{1 - x_C} \quad u_{Fe} = \frac{x_{Fe}}{x_{Cr} + x_{Fe}} \quad u_C = \frac{x_C}{x_{Cr} + x_{Fe}}$$

$$u_{Cr} + u_{Fe} = 1$$

$$c_k = u_k / V_S \quad [\text{mol/m}^3]$$

# Results – diffusion through a tube wall





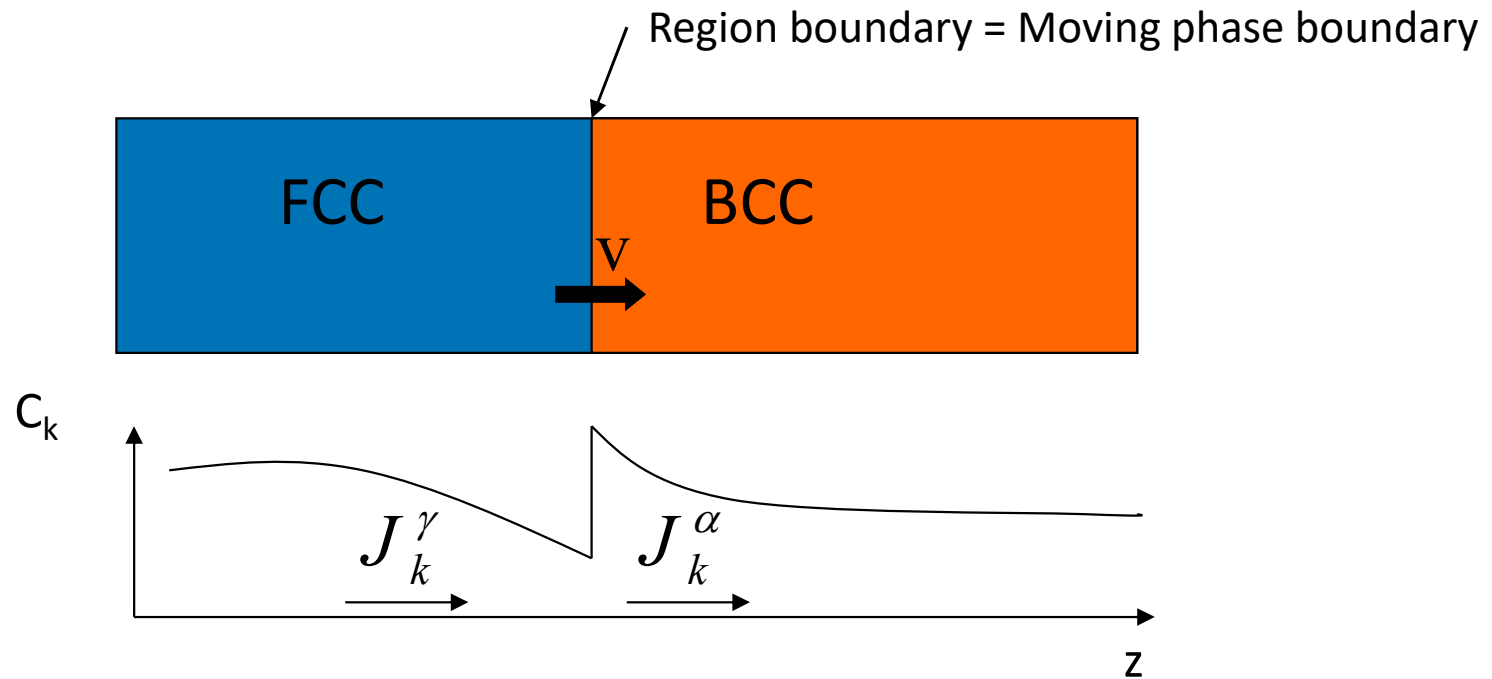
# Moving Phase boundary Example

- Growth of a particle

# Moving Phase Boundary Calculations

- ❑ Used for calculating growth or dissolution of a phase
- ❑ Assumptions:
  - ✓ Local equilibrium holds at the phase boundary, i.e. concentrations at the boundary can be calculated from an equilibrium calculation in Thermo-Calc.
  - ✓ Diffusion controls the movement of the phase boundary
- ❑ Application examples:
  - ❖ Carbide dissolution
  - ❖ Solidification
  - ❖ Growth of  $\sigma$ -phase in a stainless steel

# Moving phase boundary simulation



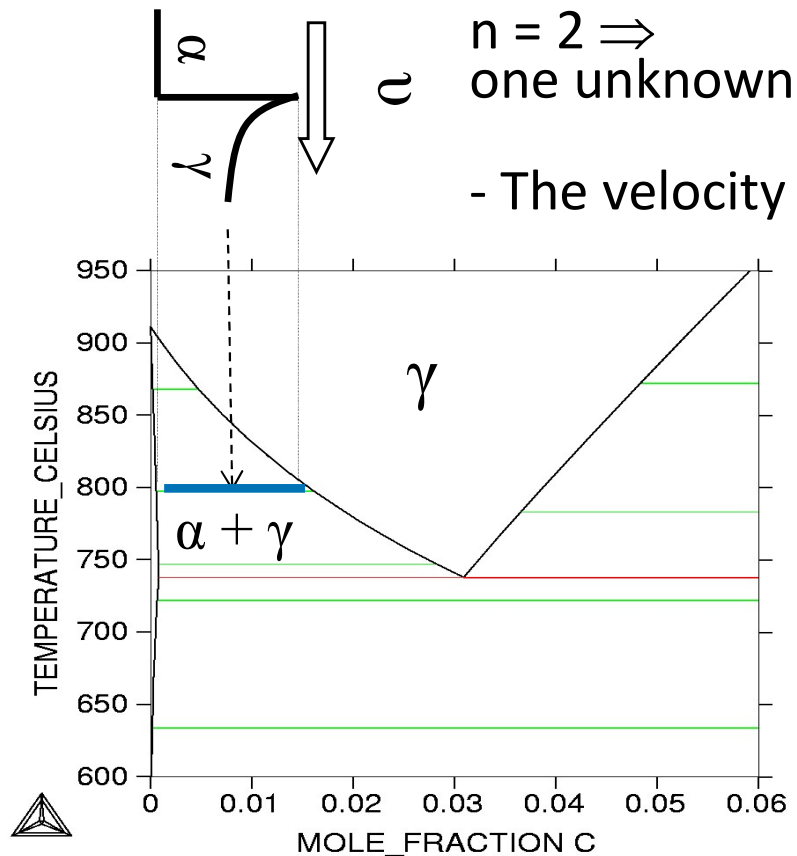
Solve diffusion equation in each phase

Calculate displacement of phase boundary

Thermo-Calc is used to find tie-lines

# Diffusion with a moving interface

## Binary example: Fe-C

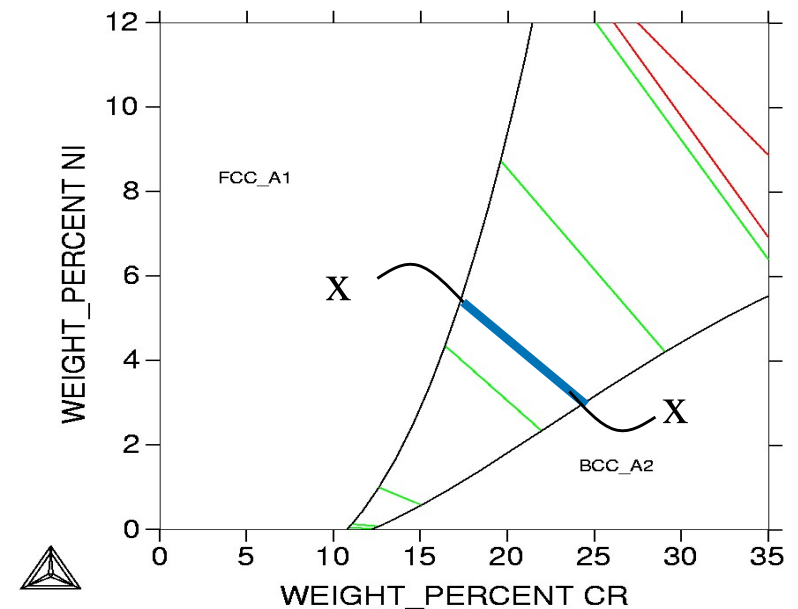


P, T const.

## Ternary example: Fe-Cr-Ni

$n = 3 \Rightarrow$  two unknowns!

- One  $a_i$  or  $\mu_i$  (i.e. one tie-line)
- The velocity



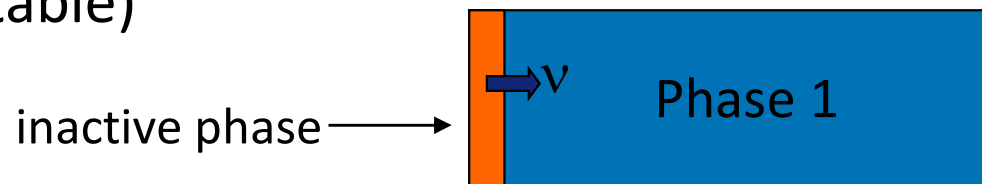
# Moving Phase Boundary

- Moving phase boundary simulations may be set up in DICTRA in two different ways:

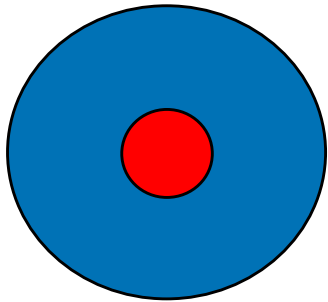
1) Introducing two or more adjacent regions containing different phases



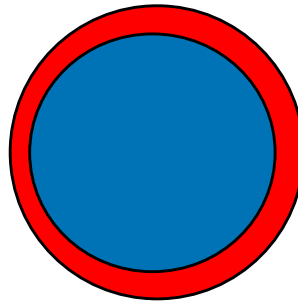
2) Entering an inactive phase (formed when thermodynamically stable)



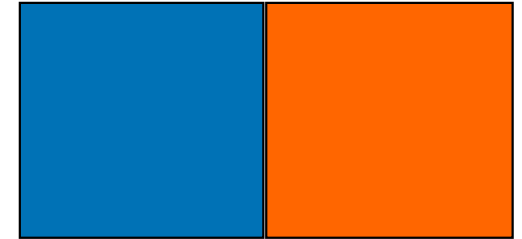
# Some possible geometries



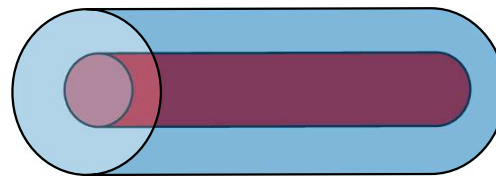
**Growth or dissolution of a spherical precipitate**



**Growth of spherical film  
(Grain-boundary film)**



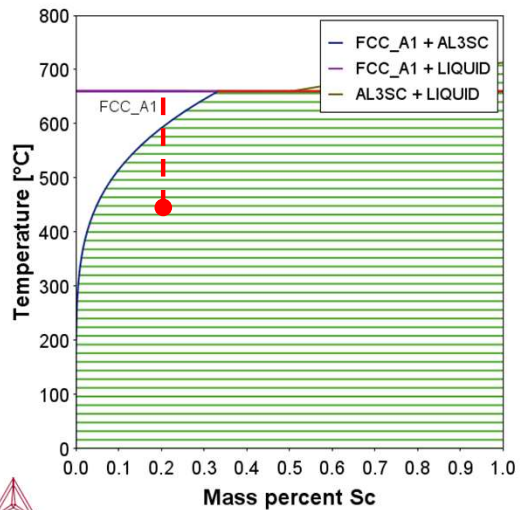
**Planar growth**



**Growth of cylindrical precipitate**

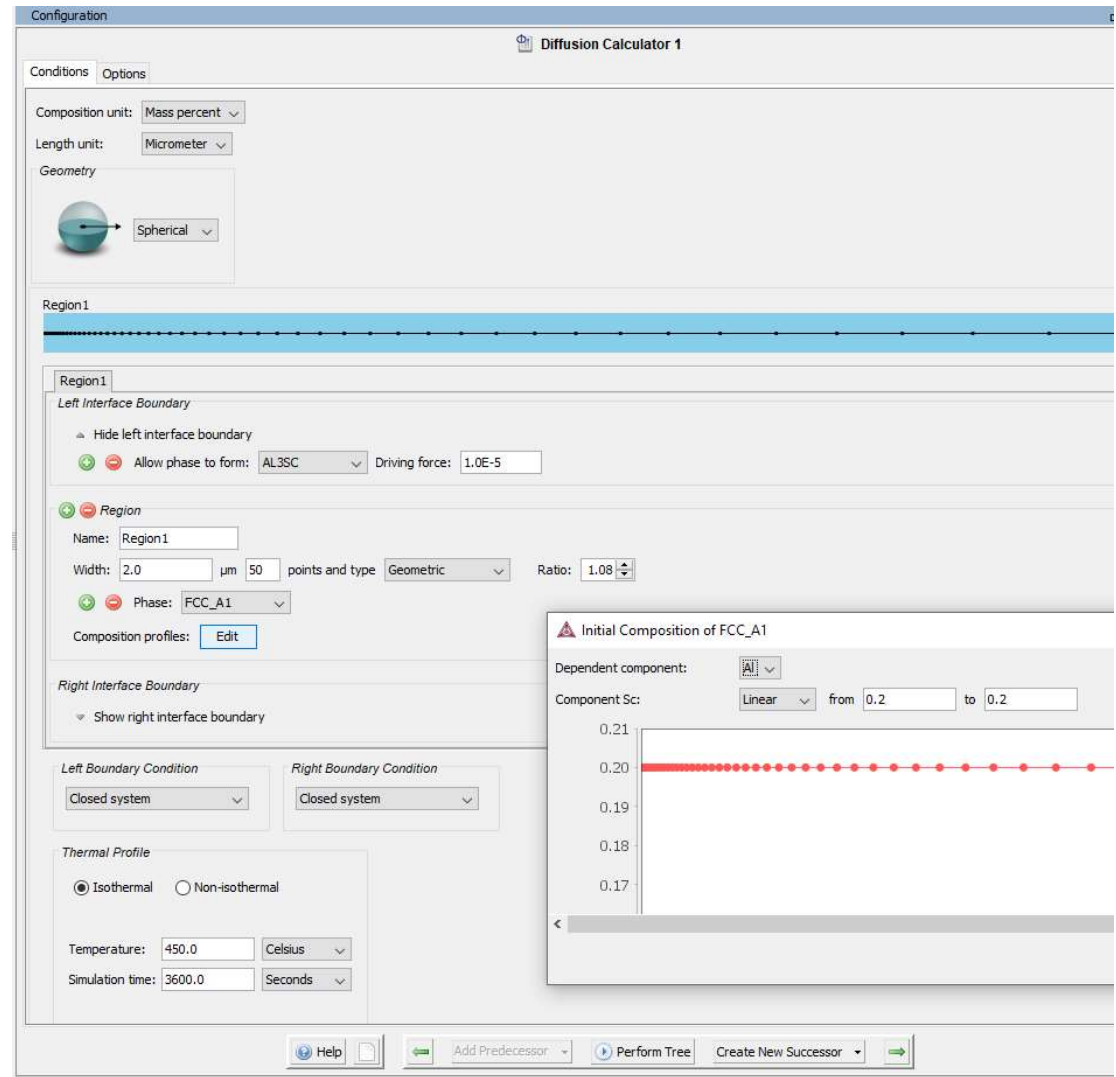
# Example: Particle growth

Al – 0.2 wt-% Sc

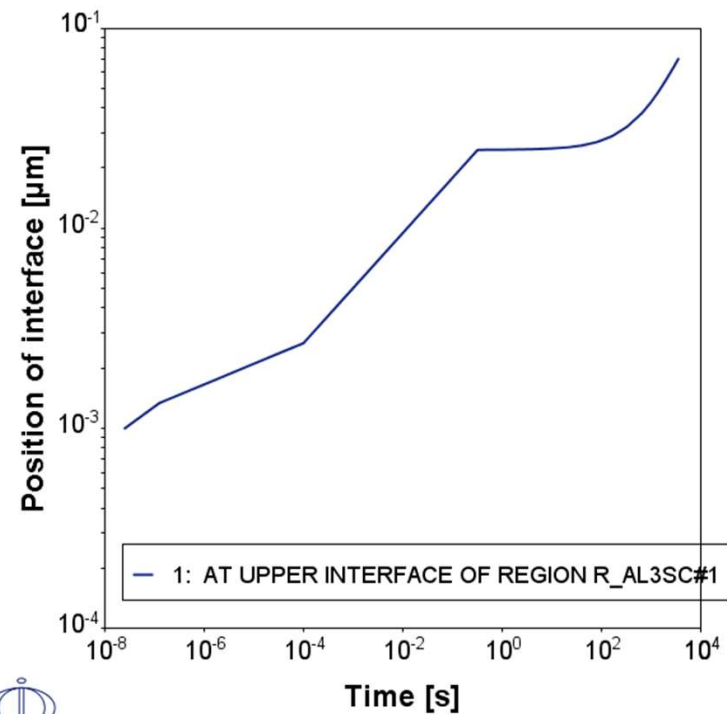
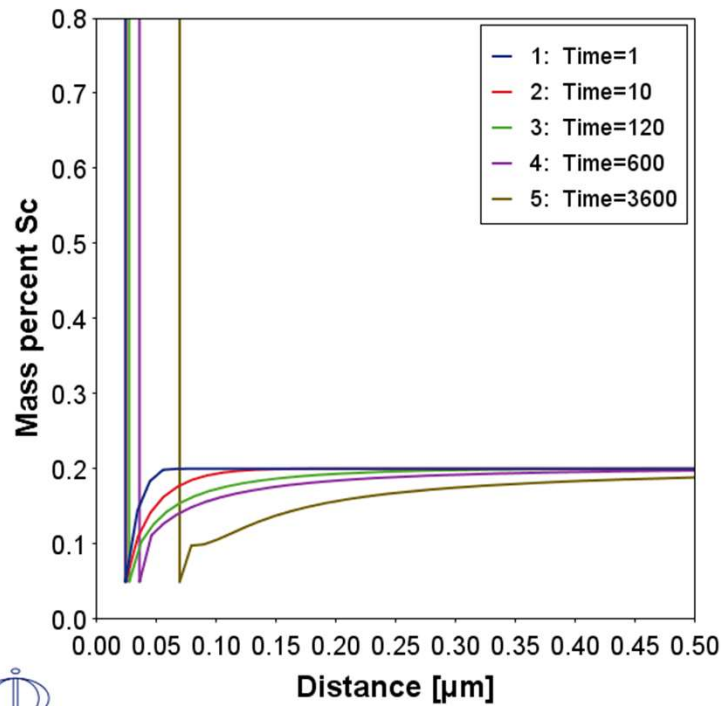
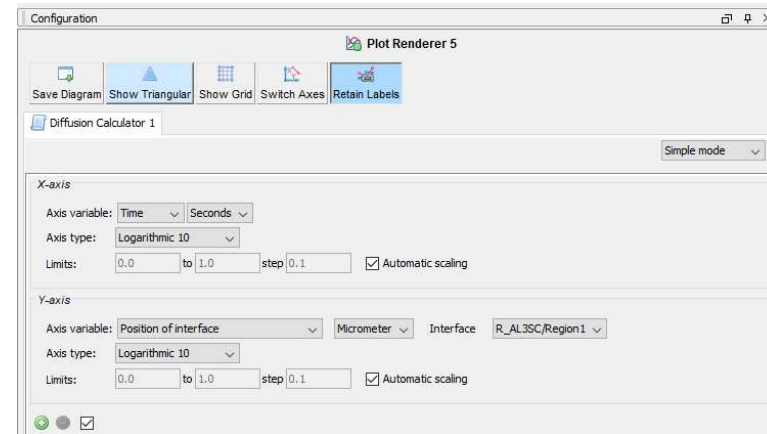
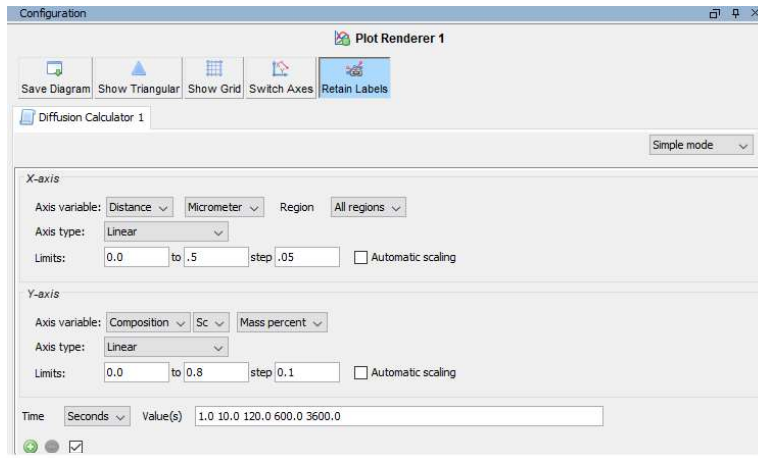


Quench to 450°C.

- Supersaturated FCC
- Driving force for the precipitation of  $\text{Al}_3\text{Sc}$
- Diffusion controlled growth of  $\text{Al}_3\text{Sc}$



# Results: Particle growth

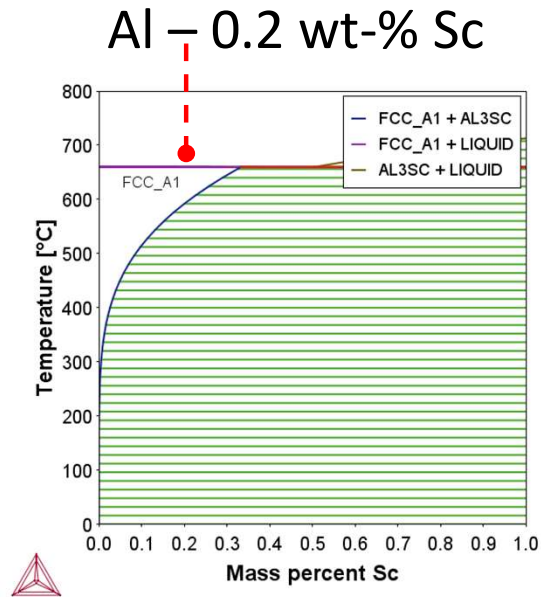




# Q & A

# Home assignment 1

# Home assignment 1: Particle growth



Try to make the Al-Sc simulation we just performed more realistic by adding the cooling from single-phase FCC at 600 °C to 450 °C.

Let's assume this cooling takes 2 seconds.

Does this change how much the phase interface has moved after 1 hour?

- 1) You have to change the setting to non-isothermal.
- 2) Also consider how you can compare the two results after time=3600 s.